



Notes 5 – Modern Lubrication

Hydrodynamic fluid film bearings and their effect on the stability of rotating machinery

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Lubricated Journal Bearings

Radial and axial load support of rotating machinery
– low friction and long life

Advantages

Do not require external source of pressure.

Support heavy loads. The load support is a function of the lubricant viscosity, surface speed, surface area, film thickness and geometry of the bearing.

Long life (infinite in theory) without wear of surfaces.

Provide stiffness and damping coefficients of large magnitude.

Disadvantages

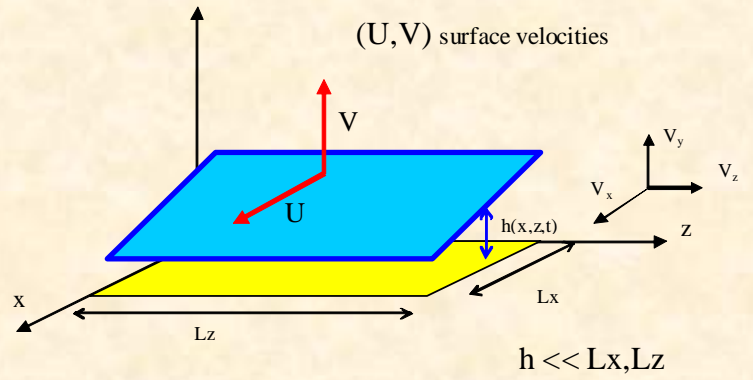
Thermal effects affect performance if film thickness is too small or available flow rate is too low.

Potential to induce **hydrodynamic instability**, i.e. loss of effective damping for operation well above critical speed of rotor-bearing system

Typically use MINERAL OIL as lubricant. Modern trend is to replace with working fluid (water)

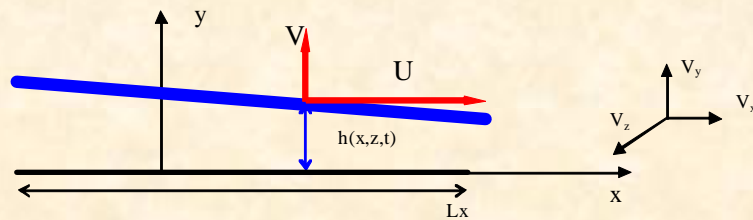


Fundamentals of Thin Film Lubrication



- Film thickness \ll other dimensions
- No curvature effects
- Laminar flow, inertialess

TYP $(c/L^*) = 0.001$



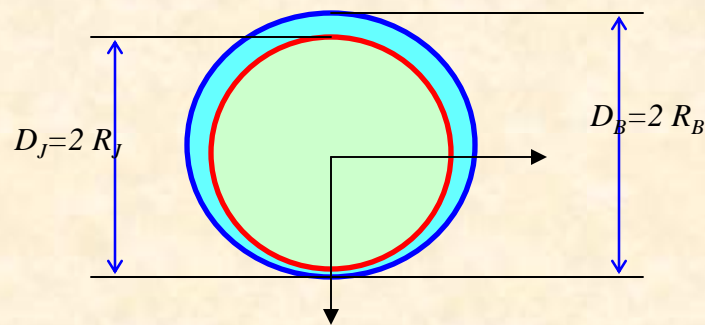
$$Re = \frac{\rho U_* c}{\mu}$$

SMALL Couette flow Reynolds #

Flow equations: continuity + momentum (x,y)

$$\frac{\partial(v_x)}{\partial x} + \frac{\partial(v_y)}{\partial y} + \frac{\partial(v_z)}{\partial z} = 0$$

$$0 = -\frac{\partial P}{\partial x} + \mu \frac{\partial^2 v_x}{\partial y^2}; \quad 0 = -\frac{\partial P}{\partial z} + \mu \frac{\partial^2 v_x}{\partial y^2}$$



Cylindrical bearing

Quasi-static (pressure forces = viscous forces)



Importance of fluid inertia in thin film flows

Reynolds numbers

fluid	Absolute viscosity (μ) lbm.ft.s x 10^{-5}	Kinematic viscosity (ν) centistoke	Re at 1,000 rpm	Re at 10,000 rpm
Air	1.23	15.4	9.9	99
Thick oil	1,682	30.0	5.1	51
Light oil	120	2.14	71	711
Water	64	1.00	159	1,588
Liquid hydrogen	1.075	0.216	705	7,052
Liquid oxygen	10.47	0.191	794	7,942
Liquid nitrogen	13.93	0.179	848	8,477
R134 refrigerant	13.30	0.163	930	9,296

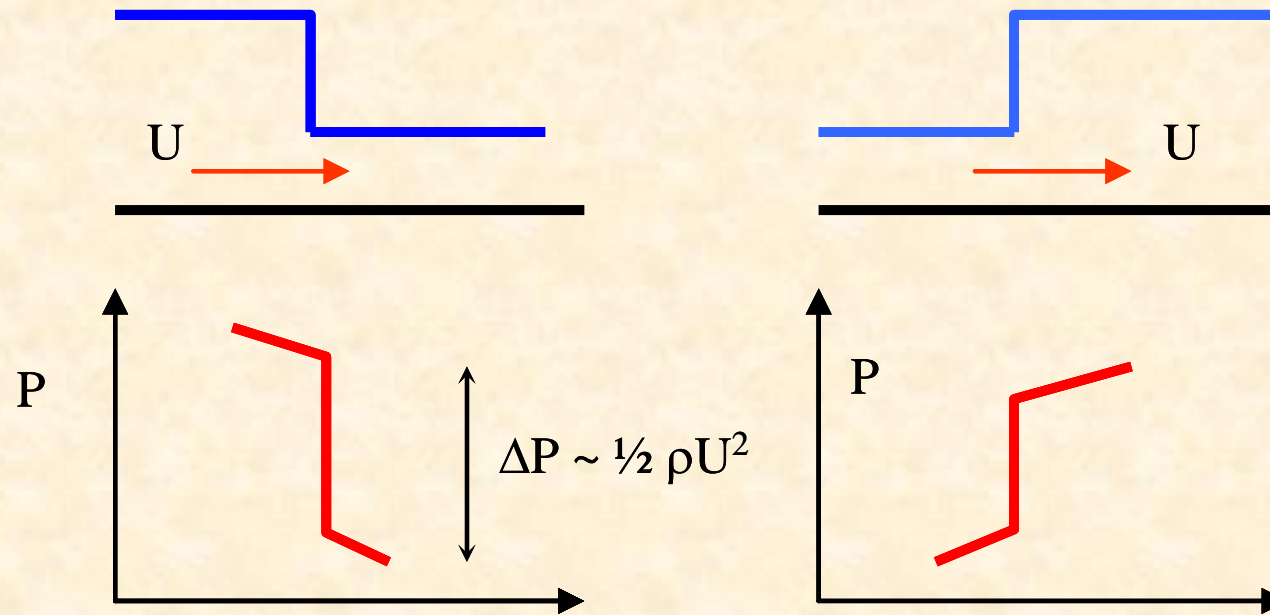
Fluid inertia is important for operation at high speeds and with process fluids. These are prevalent conditions in HP turbomachinery

Importance of fluid inertia effects on several fluid film bearing applications. $(c/R_j)=0.001$, $R_j=38.1$ mm (1.5 inch)

Table 1



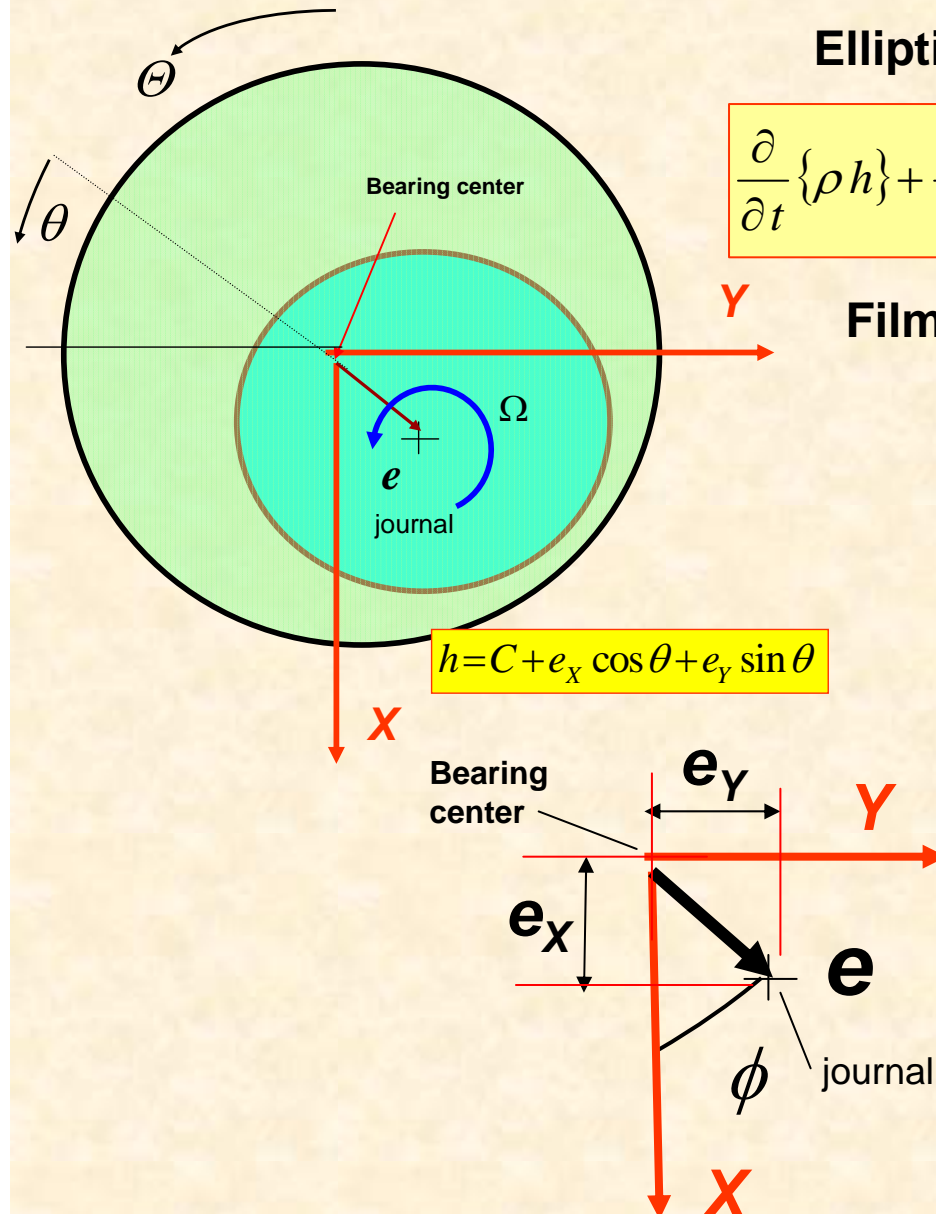
Fluid inertia effects at inlet & edges



Fluid inertia (Bernoulli's effect) causes sudden pressure drop (or raise) at sharp inlets (exits). Most important effect on annular pressure seals and hydrostatic bearings with process fluids



Thin Film Lubrication: Reynolds Equation



Elliptical PDE in film region

$$\frac{\partial}{\partial t} \{ \rho h \} + \frac{\Omega}{2} \frac{\partial}{\partial \Theta} \{ \rho h \} = \frac{1}{R^2} \frac{\partial}{\partial \Theta} \left\{ \frac{\rho h^3}{12 \mu} \frac{\partial P}{\partial \Theta} \right\} + \frac{\partial}{\partial z} \left\{ \frac{\rho h^3}{12 \mu} \frac{\partial P}{\partial z} \right\}$$

Film thickness

$$h = c + e_x \cos \Theta + e_y \sin \Theta = e \sin \theta$$

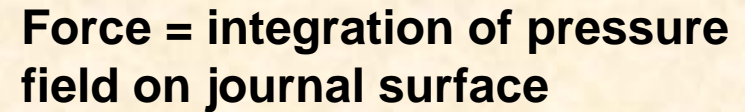
Pressure = ambient on sides
Pressure > $P_{\text{cavitation}}$

$$h = C + e_x \cos \theta + e_y \sin \theta$$

Kinematics of journal motion:

$$e_x = e \cos(\phi); \quad e_y = e \sin(\phi)$$

Figure 4 Cylindrical journal bearing & coordinates



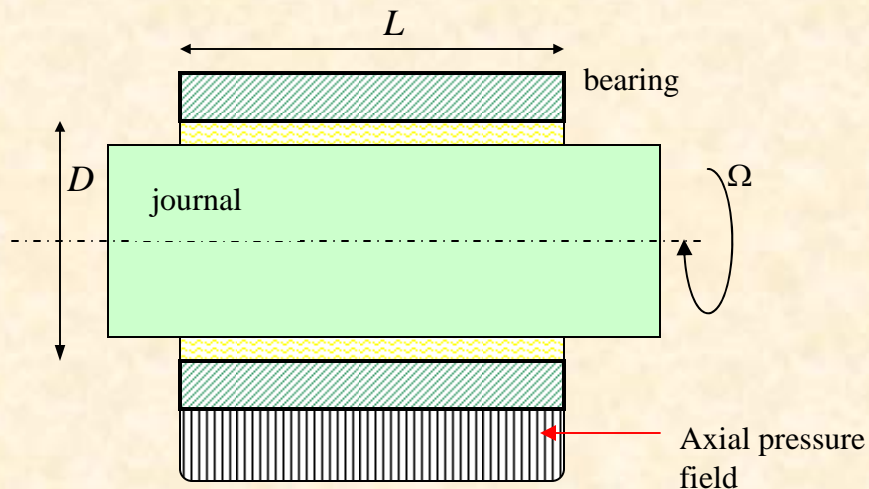
$$\begin{bmatrix} F_x \\ F_y \end{bmatrix} = \begin{bmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{bmatrix} \begin{bmatrix} F_r \\ F_t \end{bmatrix}$$



$$F_\alpha = F_\alpha(\Omega, \dot{e}_X, \dot{e}_Y) = F_\alpha\left(\dot{e}, e\left[\dot{\phi} - \frac{\Omega}{2}\right]\right)$$



LONG journal bearing (limit geometry)



$$L/D \gg \gg 1$$

$$\frac{\partial}{\partial t} \{h\} + \frac{\Omega}{2} \frac{\partial}{\partial \Theta} \{h\} = \frac{\partial}{\partial z} \left\{ \frac{h^3}{12\mu} \frac{\partial P}{\partial z} \right\}$$

LONG BEARING MODEL

$$L/D \gg 1$$

$$dP/dz \rightarrow 0$$

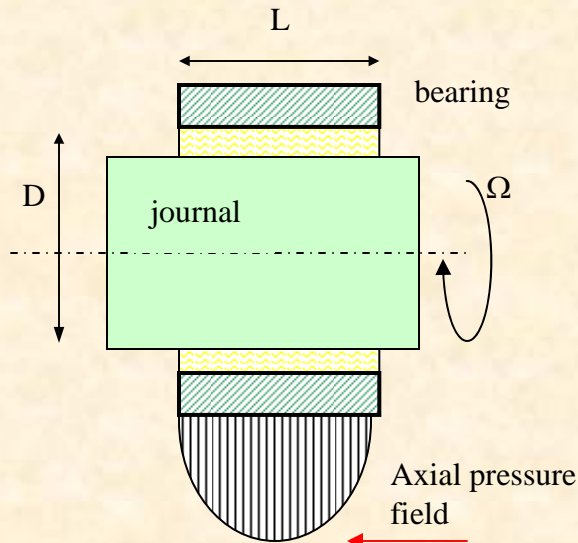


Pressure does not vary axially.
Not applicable for most practical
cases, except sealed squeeze
film dampers

Figure 6



SHORT journal bearing (limit geometry)



$$L/D \ll 1$$

$$dP/d\theta \rightarrow 0$$

$$L/D < 0.50$$

$$\frac{1}{R^2} \frac{\partial}{\partial \theta} \left\{ \frac{h^3}{12\mu} \frac{\partial P}{\partial \theta} \right\} = \frac{\partial}{\partial t} \{h\} + \frac{\Omega}{2} \frac{\partial}{\partial \Theta} \{h\}$$

Applicable to actual rotating machinery

SHORT JOURNAL BEARING MODEL

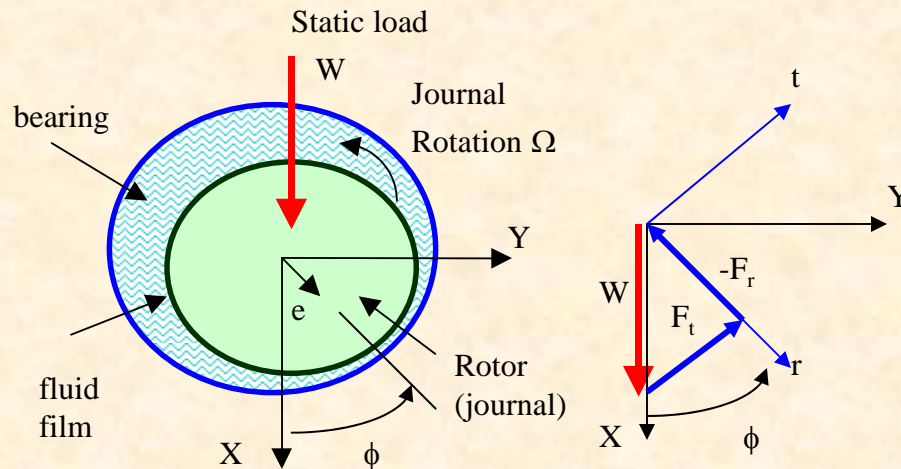
$$P(\theta, z, t) - P_a = \frac{6\mu \left[\dot{e} \cos \theta + e \left(\dot{\phi} - \frac{\Omega}{2} \right) \sin \theta \right]}{C^3 H^3} \left\{ z^2 - \left(\frac{L}{2} \right)^2 \right\}$$

Hydrodynamic pressure is proportional to viscosity (μ), speed (Ω), and most important to: $1/C^3$

Control of tolerances in machined clearance is critical for reliable performance



STATIC LOAD PERFORMANCE



Force Balance for Static Load

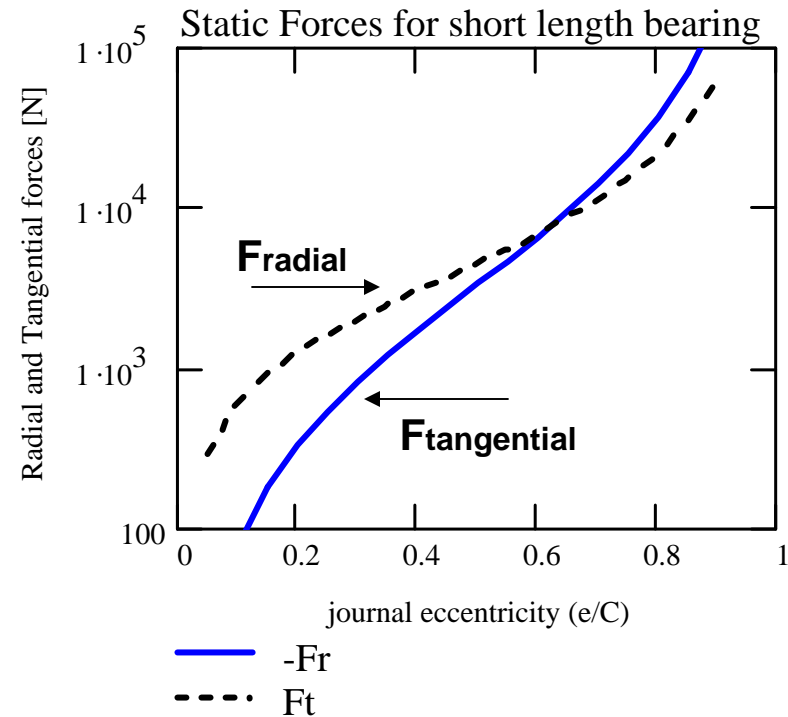
Radial and tangential forces for
 $L/D=0.25$ bearing. $\mu=0.019$ Pa.s, $L=0.05$
 m, $c=0.1$ mm, 3, 000 rpm,



Journal bearing can generate large reaction forces. Highly nonlinear functions of journal eccentricity

Bearing reaction force = applied static load (% of rotor weight)

$$F_r = -\frac{\mu R L^3 \Omega}{c^3} \frac{\varepsilon^2}{(1-\varepsilon^2)^2}; \quad F_t = +\frac{\mu R L^3 \Omega}{c^2} \frac{\pi \cdot \varepsilon}{4(1-\varepsilon^2)^{3/2}}$$



*



DESIGN PARAMETER: STATIC LOAD PERFORMANCE

Sommerfeld number

$$S = \frac{\mu N L D}{W} \left(\frac{R}{c} \right)^2$$

N rotational speed (rev/s)

W static load

$L, D=2R, c$: clearance &

μ viscosity

Given S , iterative solution to find operating journal eccentricity ($\varepsilon = e/c$) and attitude angle (ϕ):

$$\sigma = \pi S (L/D)^2 = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2 = \frac{(1-\varepsilon^2)^2}{\varepsilon \sqrt{16\varepsilon^2 + \pi^2(1-\varepsilon^2)}}$$

$$\tan \phi = - \frac{F_t}{F_r} = \frac{\pi \sqrt{1-\varepsilon^2}}{4 \varepsilon}$$

Attitude angle

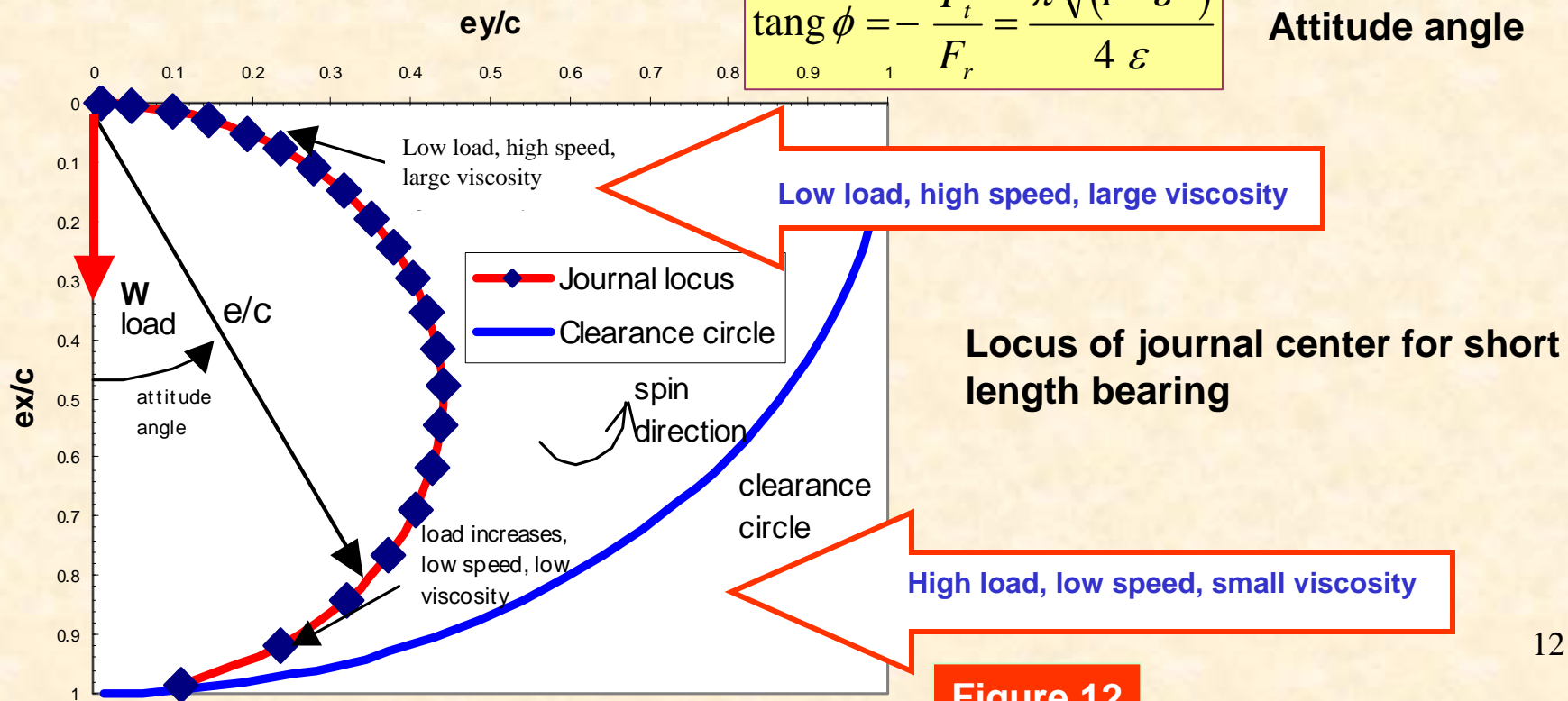


Figure 12



DESIGN PARAMETER: STATIC LOAD PERFORMANCE

Sommerfeld number

$$\sigma = \pi S (L/D)^2 = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$

N rotational speed (rev/s)

W static load

$L, D=2R, c$: clearance &

μ viscosity

σ

Sommerfeld number

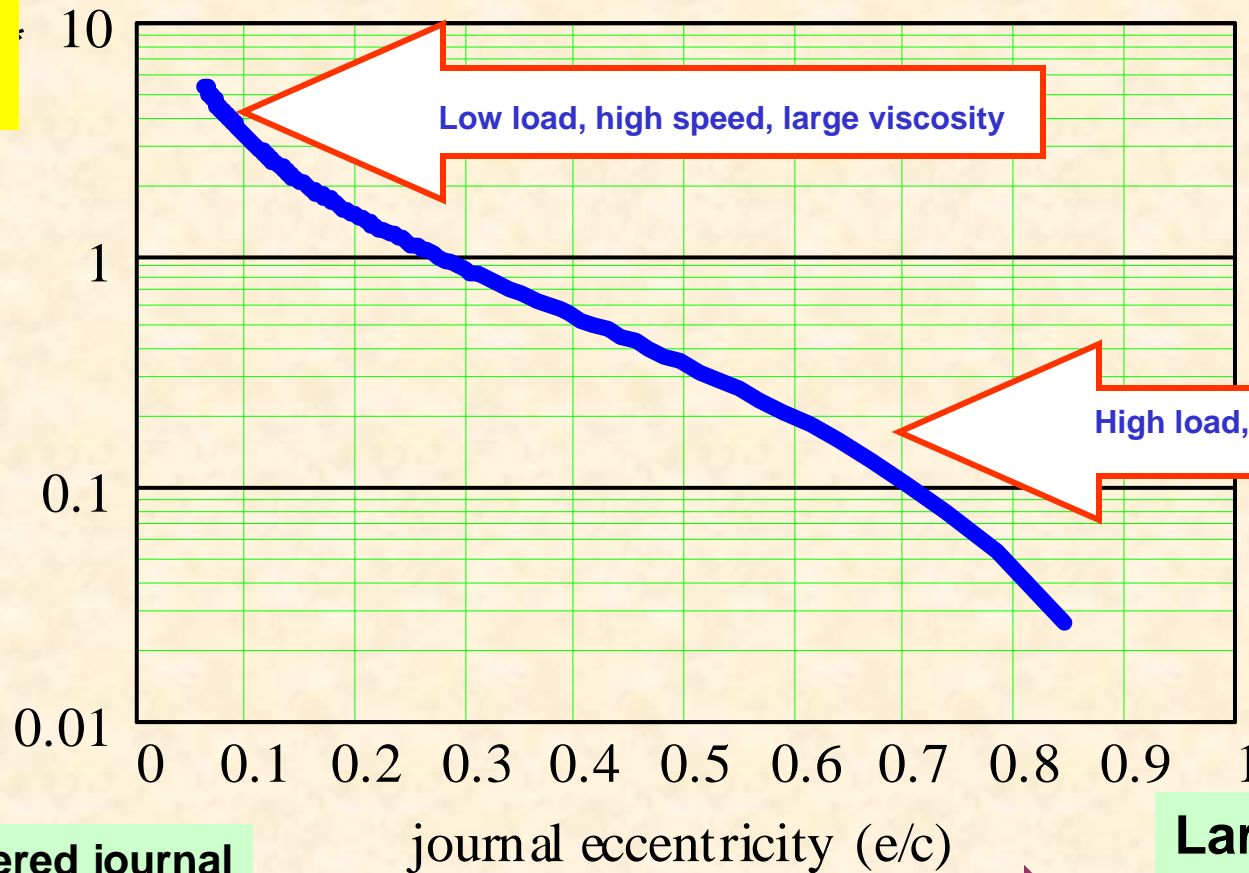


Figure 10 Sommerfeld # vs journal eccentricity



DESIGN PARAMETER: STATIC LOAD PERFORMANCE

Sommerfeld number

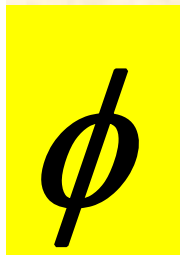
$$\sigma = \pi S (L/D)^2 = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$

N rotational speed (rev/s)

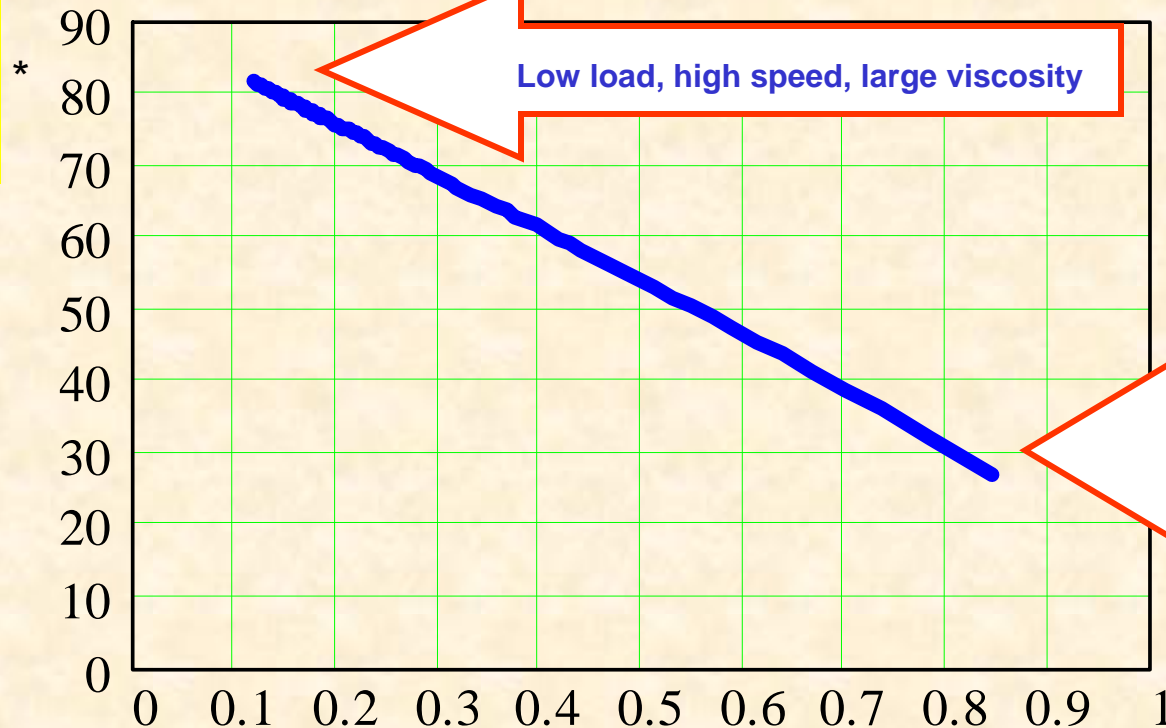
W static load

$L, D=2R, c$: clearance &

μ viscosity



Attitude angle



Centered journal

journal eccentricity (e/c)

Large e

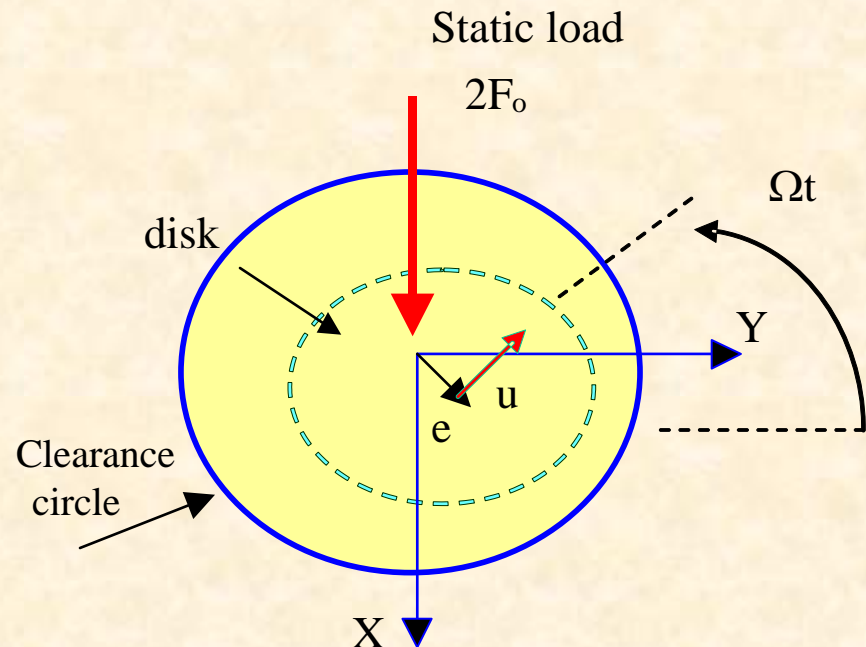
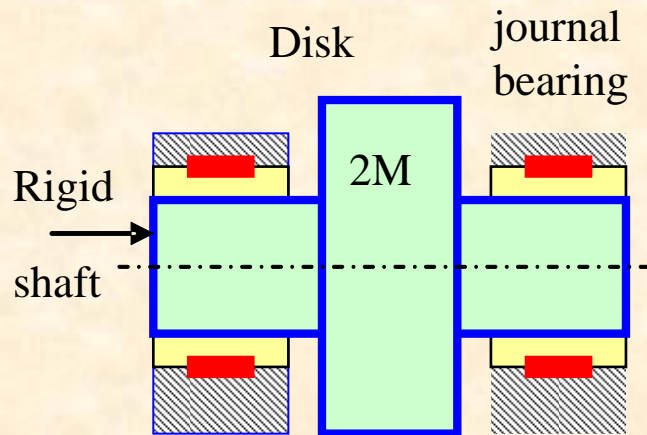


Figure 11 Attitude angle # vs journal eccentricity

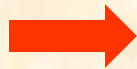


DYNAMICS OF ROTOR-BEARING SYSTEM

Symmetric - rigid rotor supported on short length journal bearings



Equations of motion:



$$M \ddot{X} = F_X + M u \Omega^2 \sin(\Omega t) + F_o$$

$$M \ddot{Y} = F_Y + M u \Omega^2 \cos(\Omega t)$$

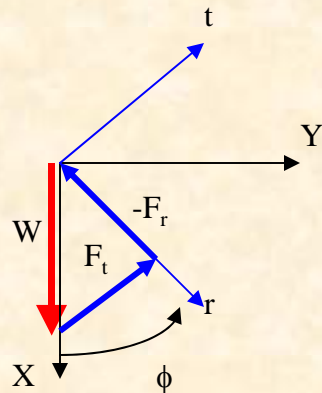
Figure 13

Rigid rotor supported on journal bearings.
(u) imbalance, (e) journal eccentricity



DYNAMICS OF ROTOR-BEARING SYSTEM

Consider small amplitude motions about static equilibrium position (SEP). SEP defined by applied static load.

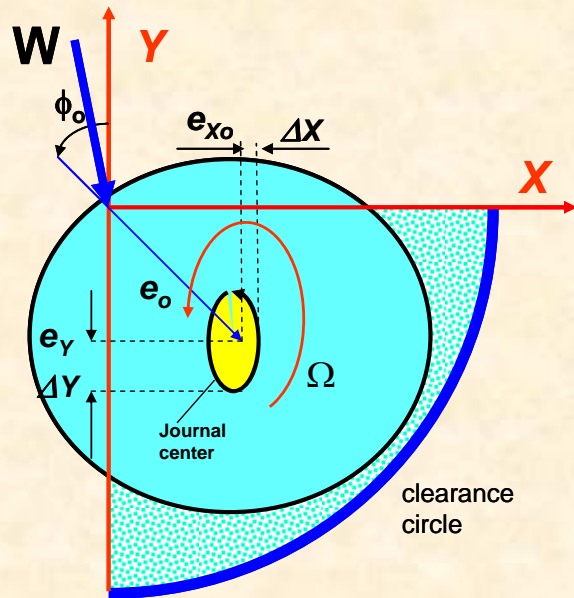


$$F_{X_o} = -F_o, \quad F_{Y_o} = 0, \quad \Rightarrow e_{X_o}, e_{Y_o} \text{ or } e_o, \phi_o$$

Let:

$$e_X = e_{X_o} + \Delta e_X(t), \quad e_Y = e_{Y_o} + \Delta e_Y(t)$$

Static load



Expansion of forces about SEP

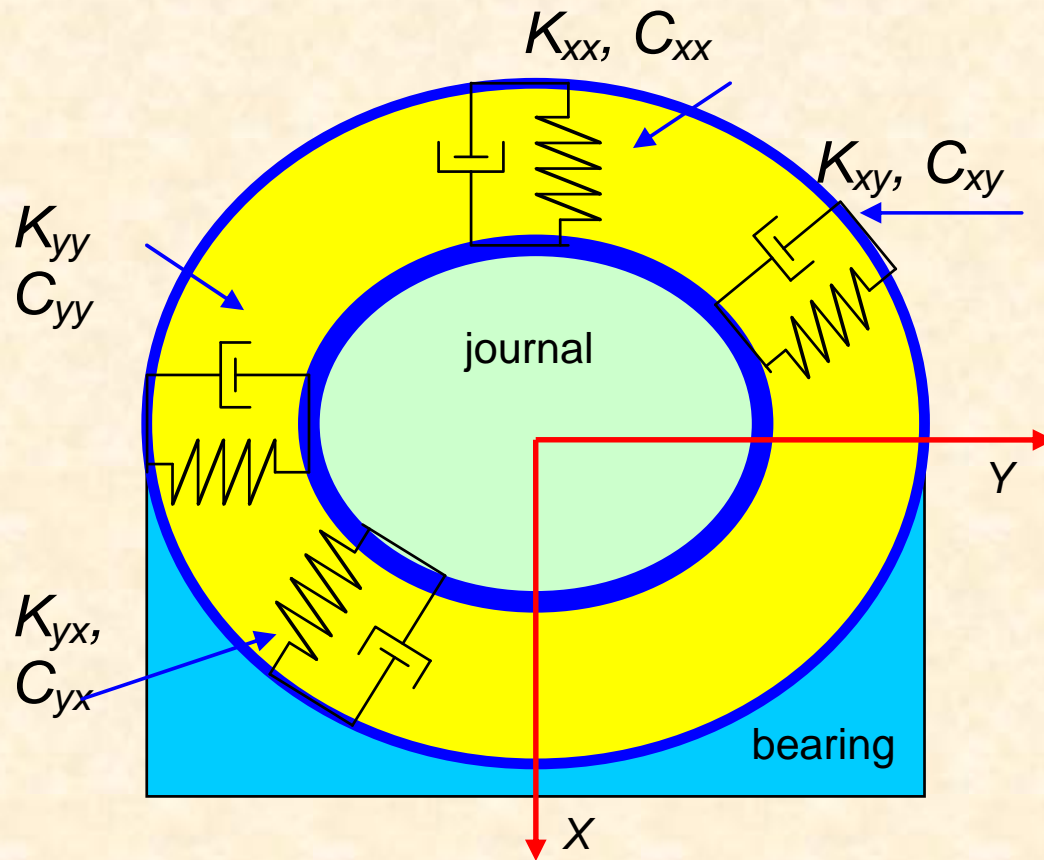
$$F_X = F_{X_o} + \frac{\partial F_X}{\partial X} \Delta X + \frac{\partial F_X}{\partial Y} \Delta Y + \frac{\partial F_X}{\partial \dot{X}} \Delta \dot{X} + \frac{\partial F_X}{\partial \dot{Y}} \Delta \dot{Y}$$

$$F_Y = F_{Y_o} + \frac{\partial F_Y}{\partial X} \Delta X + \frac{\partial F_Y}{\partial Y} \Delta Y + \frac{\partial F_Y}{\partial \dot{X}} \Delta \dot{X} + \frac{\partial F_Y}{\partial \dot{Y}} \Delta \dot{Y}$$

Figure 14 Small amplitude journal motions about an equilibrium position



ROTORDYNAMIC FORCE COEFFICIENTS



Stiffness:

$$\rightarrow K_{ij} = -\frac{\partial F_i}{\partial X_j} ;$$

Damping:

$$\rightarrow C_{ij} = -\frac{\partial F_i}{\partial \dot{X}_j}$$

Inertia:

$$\rightarrow M_{ij} = -\frac{\partial F_i}{\partial \ddot{X}_j} ;$$

$i, j = X, Y$

Strictly valid for small
amplitude motions. Derived
from SEP

The “physical representation” of stiffness
and damping coefficients in lubricated
bearings

Figure 15



ROTOR DYNAMIC FORCE COEFFICIENTS

Static reaction force:

Stiffness Matrix:

Damping Matrix:

$$\begin{pmatrix} F_X(t) \\ F_Y(t) \end{pmatrix} = \begin{bmatrix} F_{X_o} \\ F_{Y_o} \end{bmatrix} - \begin{bmatrix} K_{XX} & K_{XY} \\ K_{YX} & K_{YY} \end{bmatrix} \begin{pmatrix} \Delta X \\ \Delta Y \end{pmatrix} - \begin{bmatrix} C_{XX} & C_{XY} \\ C_{YX} & C_{YY} \end{bmatrix} \begin{pmatrix} \Delta \dot{X} \\ \Delta \dot{Y} \end{pmatrix}$$



Inertia ~ 0 in journal bearings

Linearized Equations of motion

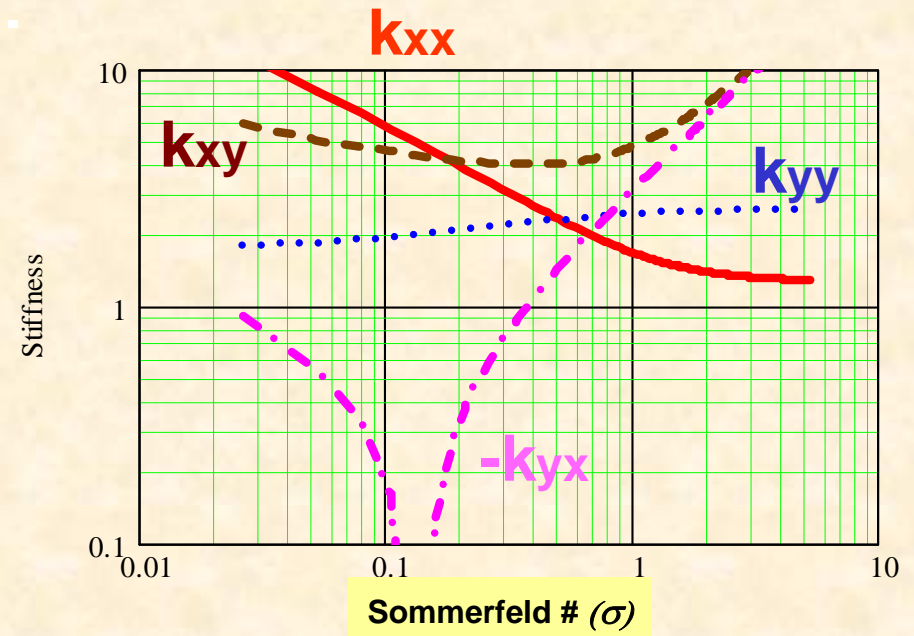
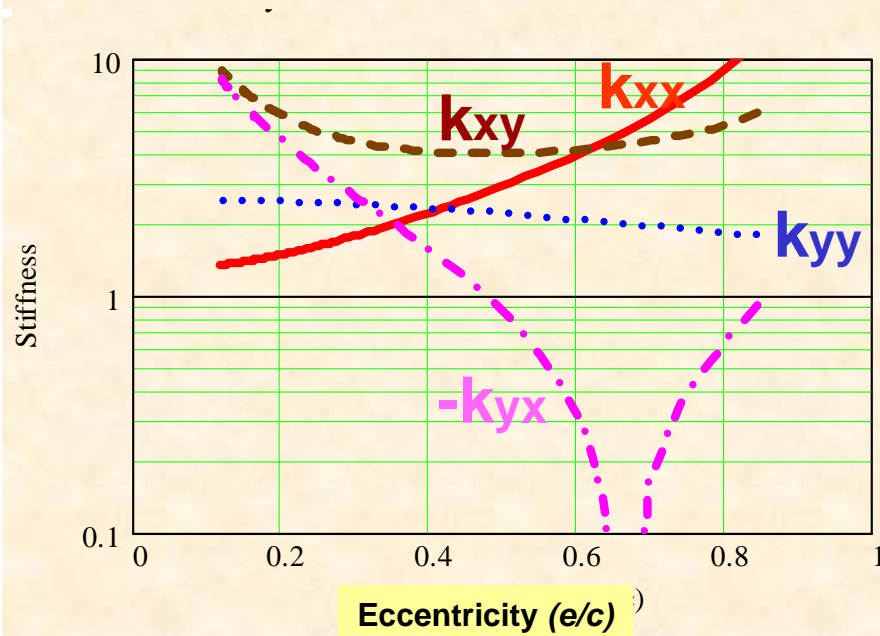
$$\begin{bmatrix} M & O \\ O & M \end{bmatrix} \begin{pmatrix} \Delta \ddot{X} \\ \Delta \ddot{Y} \end{pmatrix} + \begin{bmatrix} C_{XX} & C_{XY} \\ C_{YX} & C_{YY} \end{bmatrix} \begin{pmatrix} \Delta \dot{X} \\ \Delta \dot{Y} \end{pmatrix} + \begin{bmatrix} K_{XX} & K_{XY} \\ K_{YX} & K_{YY} \end{bmatrix} \begin{pmatrix} \Delta X \\ \Delta Y \end{pmatrix} = M u \Omega^2 \begin{pmatrix} \cos \Omega t \\ \sin \Omega t \end{pmatrix}$$

Strictly valid for small amplitude motions. Derived from SEP



Journal Bearing: STIFFNESS COEFFICIENTS

$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$



High speed
Low load
Large viscosity

Low speed
Large load
Low viscosity

High speed
Low load
Large viscosity

$$k_{\alpha\beta} = K_{\alpha\beta} (c/F_o)$$

Care with non dimensional value interpretation

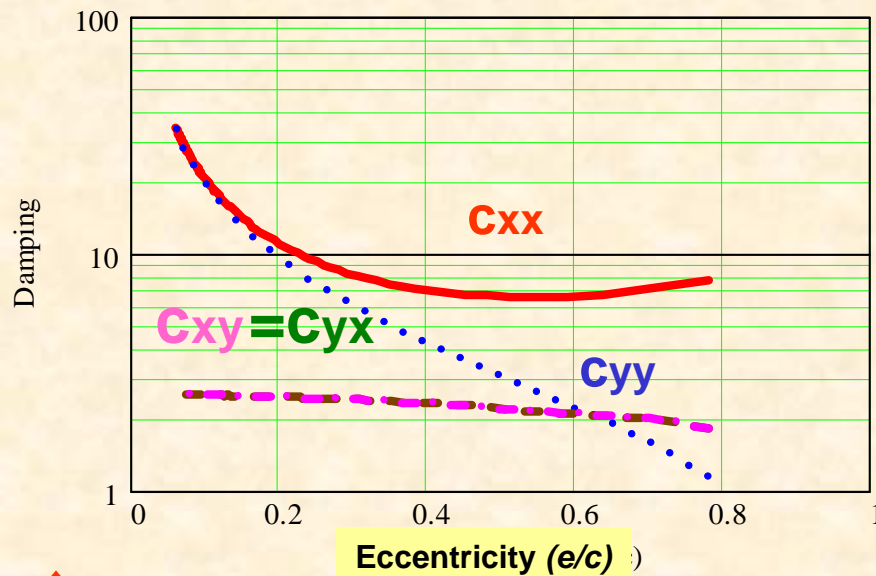
$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$

Figure 16 & 17 Bearing stiffnesses versus eccentricity and design number (σ)



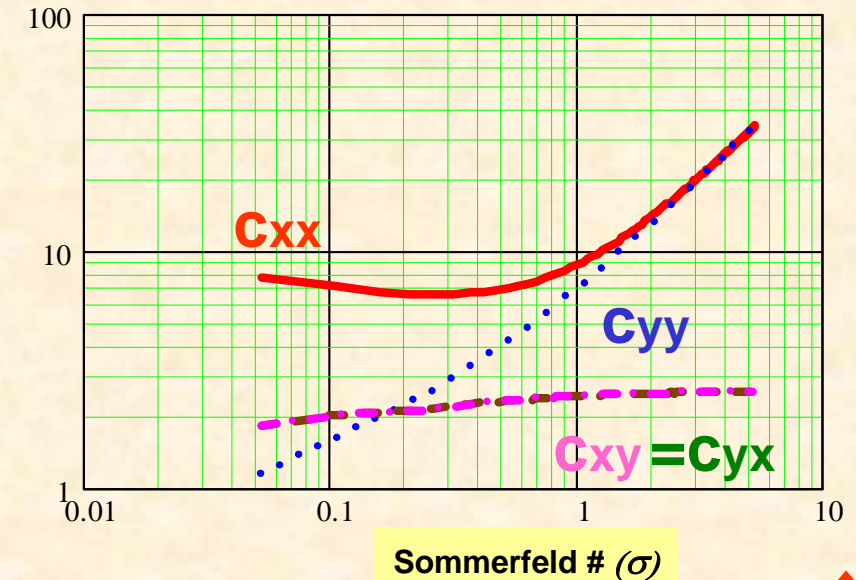
Journal Bearing: DAMPING COEFFICIENTS

$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$



↑
High speed
Low load
Large viscosity

↑
Low speed
Large load
Low viscosity



↑
High speed
Low load
Large viscosity

$$c_{\alpha\beta} = C_{\alpha\beta} (c\Omega/F_o)$$

Care with non dimensional value interpretation

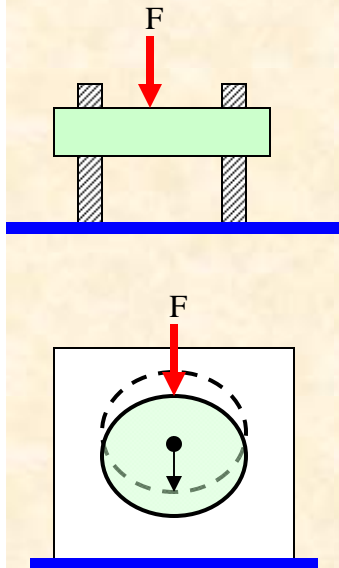
$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$

Figure 16 & 17 Bearing damping versus eccentricity and design number (σ)

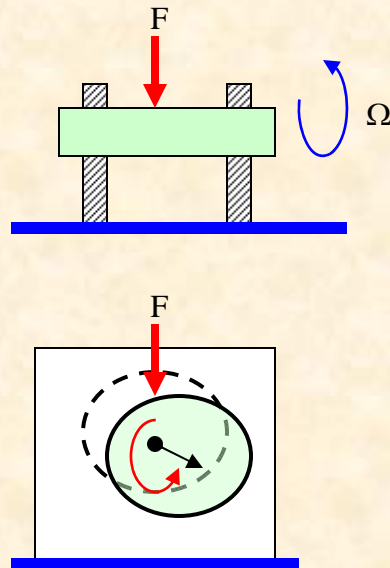


Journal Bearing: OPERATION at CENTERED CONDITION

Non-rotating structure



Rotating structure



High speed
Low load
Large viscosity

$e_o \rightarrow 0, \phi_o = 90 \text{ deg}$

$K_{xx} = K_{yy} = 0$
no direct stiffness

$K_{xy} = C_{xx} \Omega/2$

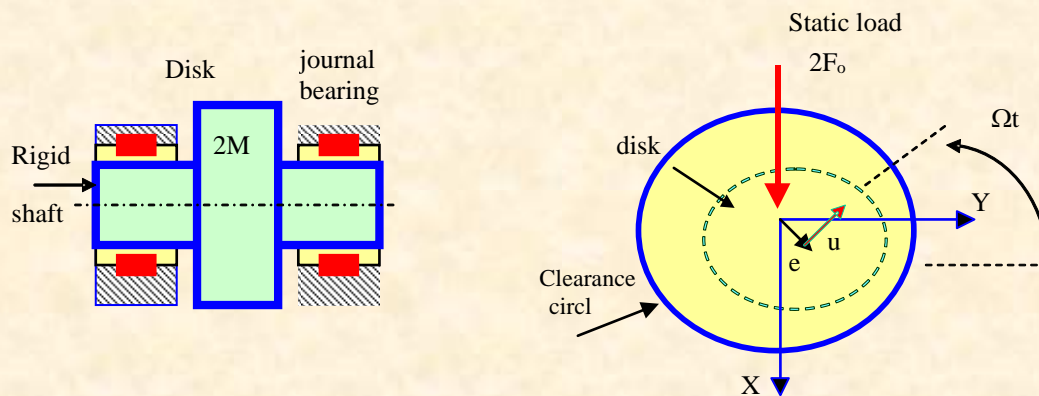
Significance of cross-coupled effect in journal bearing

$$K_{xy} = -K_{yx} = \bar{k} = \frac{\mu \Omega R L^3}{c^3} \frac{\pi}{4} = \frac{\Omega}{2} \bar{c}; \quad C_{xx} = C_{yy} = \bar{c} = \frac{\mu R L^3}{c^3} \frac{\pi}{2}$$

Pure cross-coupling effect



STABILITY OF ROTOR-BEARING SYSTEM



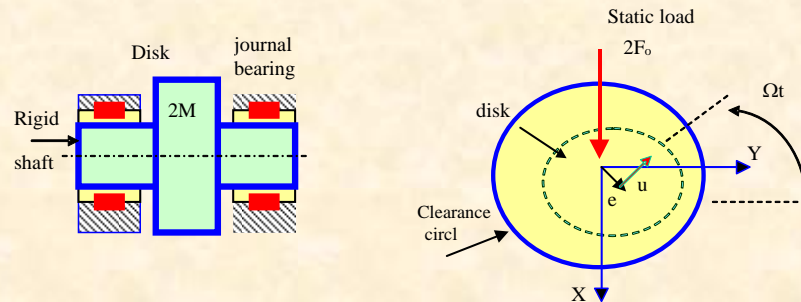
$$\begin{bmatrix} M & O \\ O & M \end{bmatrix} \begin{pmatrix} \Delta \ddot{X} \\ \Delta \ddot{Y} \end{pmatrix} + \begin{bmatrix} C_{XX} & C_{XY} \\ C_{YX} & C_{YY} \end{bmatrix} \begin{pmatrix} \Delta \dot{X} \\ \Delta \dot{Y} \end{pmatrix} + \begin{bmatrix} K_{XX} & K_{XY} \\ K_{YX} & K_{YY} \end{bmatrix} \begin{pmatrix} \Delta X \\ \Delta Y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

If rotor-bearing system is to become unstable, this will occur at a threshold speed of rotation (Ω_s) with rotor performing (undamped) orbital motions at a whirl frequency (ω_s)

$$\Rightarrow x = A e^{j\omega_s t} = A e^{j\bar{\omega}\tau} ; y = B e^{j\omega_s t} = B e^{j\bar{\omega}\tau} ; j = \sqrt{-1}$$



STABILITY OF ROTOR-BEARING SYSTEM



Equivalent support stiffness



$$p_s^2 \bar{\omega}_s^2 = k_{eq} = \frac{k_{XX} c_{YY} + k_{YY} c_{XX} - c_{YX} k_{XY} - c_{XY} k_{YX}}{c_{XX} + c_{YY}} = \frac{C M \omega_s^2}{F_o}$$

Whirl frequency ratio



$$\bar{\omega}_s^2 = \frac{(k_{eq} - k_{XX})(k_{eq} - k_{YY}) - k_{XY} \cdot k_{YX}}{c_{XX} c_{YY} - c_{XY} c_{YX}} = \left(\frac{\omega_s}{\Omega_s} \right)^2$$

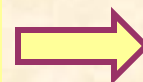
= whirl frequency (ω_s)/threshold speed instability (Ω_s)

The WFR is independent of the rotor characteristics (rotor mass and flexibility)

$$M \omega_s^2 = k_{eq} \left(\frac{F_o}{C} \right) = K_{eq}$$



$$\omega_s = \sqrt{\frac{K_{eq}}{M}} = \omega_n$$

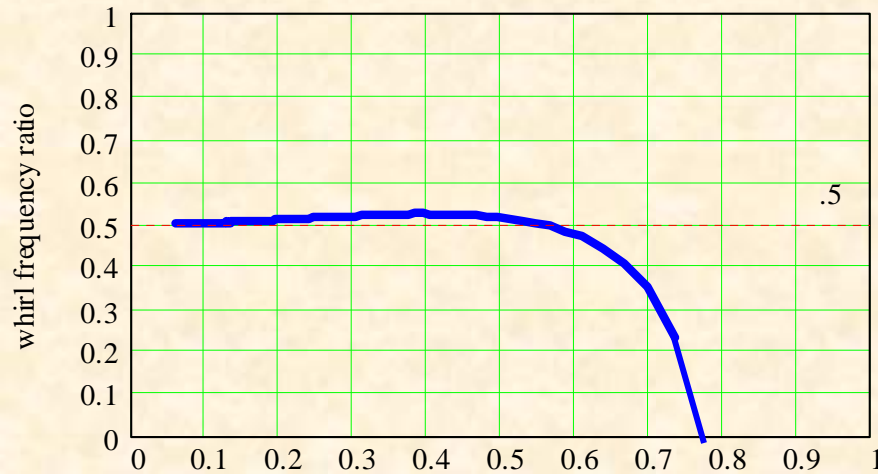


whirl frequency equals the natural frequency of rigid rotor supported on journal bearings

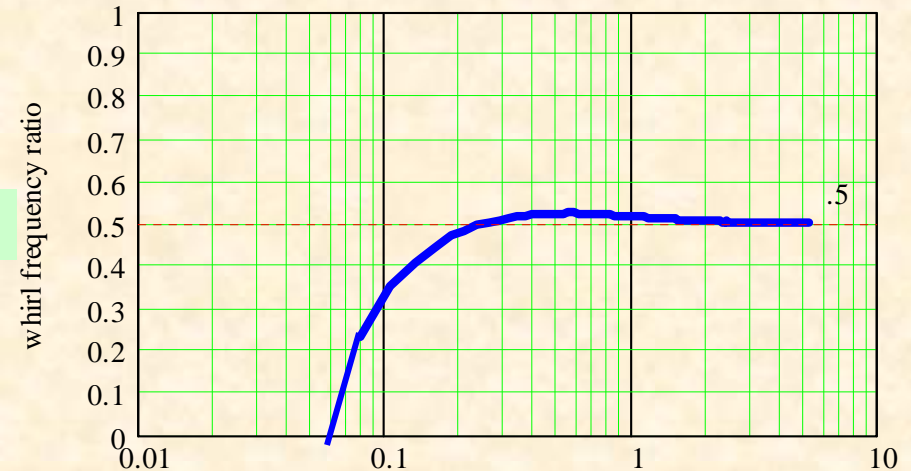


WHIRL FREQUENCY RATIO

$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$



0.50



High speed
Low load
Large viscosity

Low speed
Large load
Low viscosity

High speed
Low load
Large viscosity

At centered condition

$$k_{XX} = k_{YY} = 0; \quad c_{XX} = c_{YY}; \quad k_{XY} = -k_{YX}; \quad c_{XY} = c_{YX} = 0$$

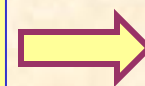
$$k_{eq} = (k_{XX} c_{XX} + c_{XY} k_{XY}) / c_{XX} = 0$$

Figure 18

Whirl
frequency
ratio



$$\frac{\omega_s}{\Omega_s} = \frac{k_{XY}}{c_{XX}} = 0.50 \quad \text{as } \varepsilon \rightarrow 0$$



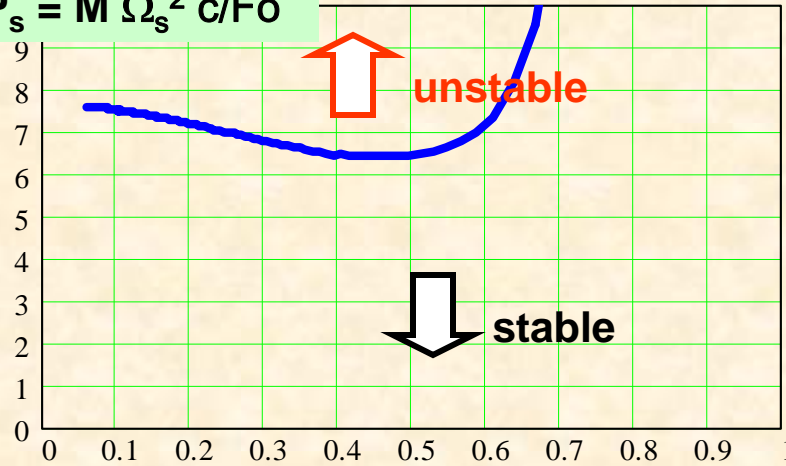
Rotor becomes
unstable at speed =
twice system
natural frequency



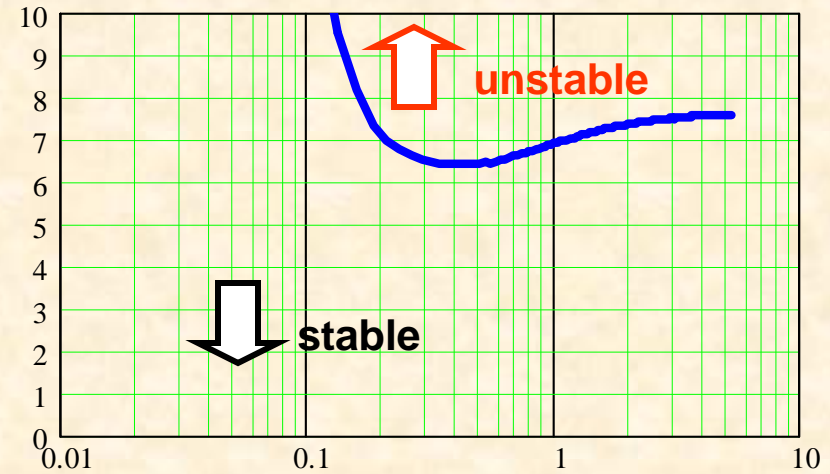
Threshold speed of instability

$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$

$$P_s = M \Omega_s^2 c / F_o$$



Eccentricity (e/c)



Sommerfeld # (σ)



High speed
Low load
Large viscosity



Low speed
Large load
Low viscosity



High speed
Low load
Large viscosity

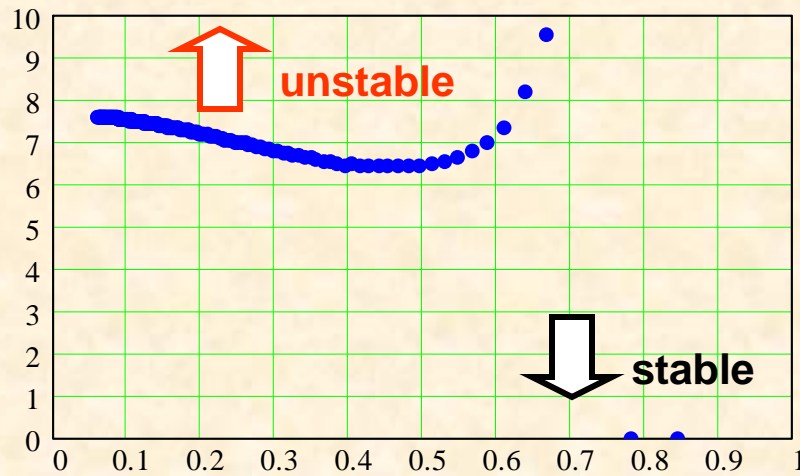


Fully stable for operation with $\varepsilon > 0.75$, all bearings (L/D).
Threshold speed decreases as eccentricity (e/c) $\rightarrow 0$

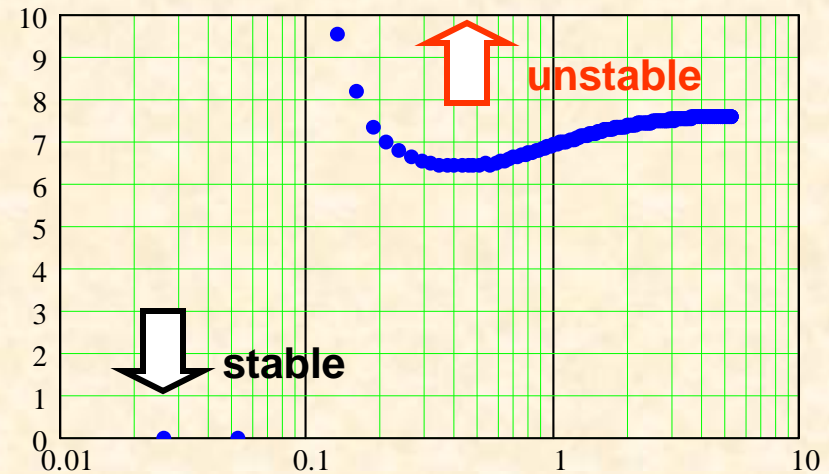


CRITICAL MASS

$$\sigma = \frac{\mu \Omega L R}{4W} \left(\frac{L}{c} \right)^2$$



Eccentricity (e/c)



Sommerfeld # (σ)



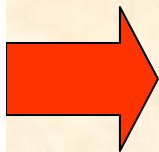
High speed
Low load
Large viscosity



Low speed
Large load
Low viscosity



High speed
Low load
Large viscosity

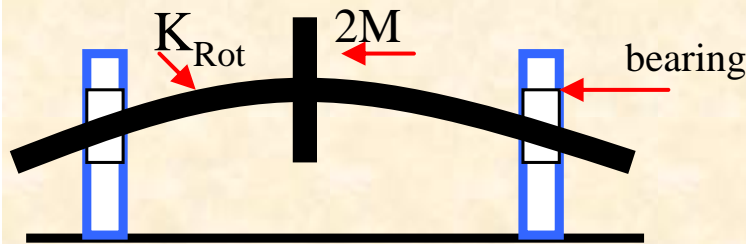


Critical mass equals maximum mass rotor is able to support stably if current operating speed = threshold speed of instability.

Critical mass decreases for centered condition. Unlimited for large (e/c)

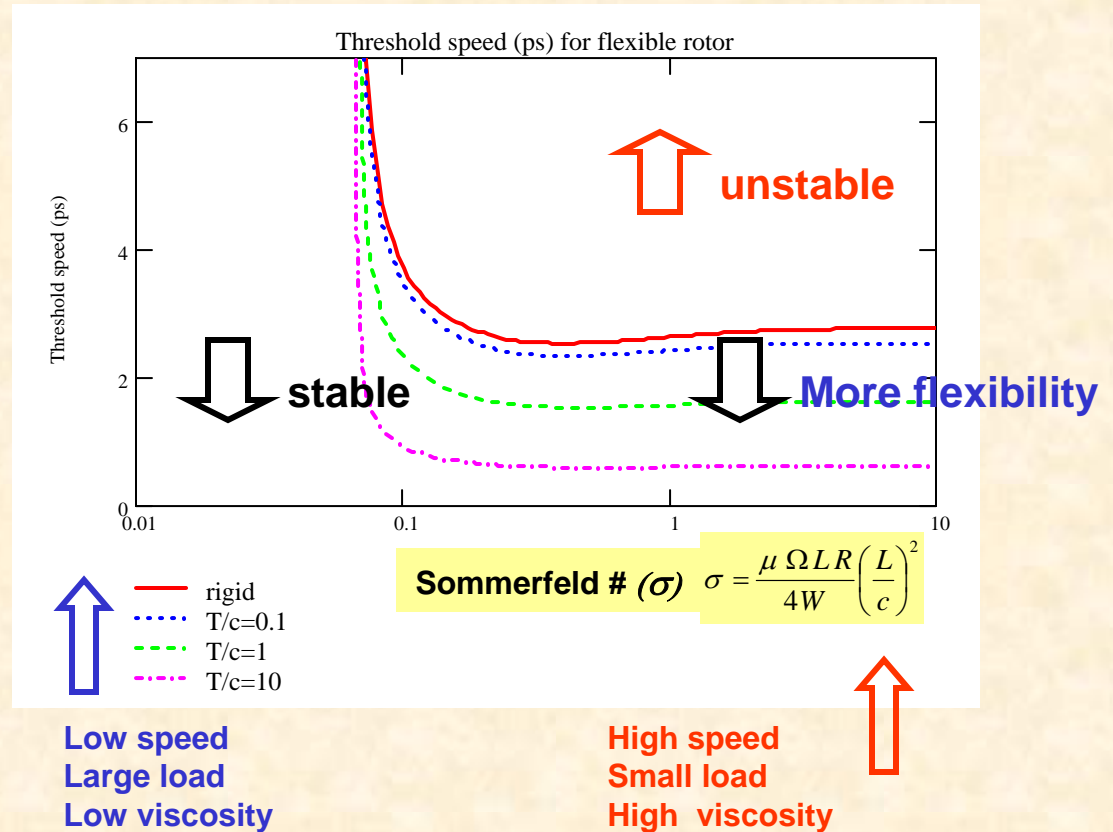


EFFECTS OF ROTOR FLEXIBILITY



$$p_{sf}^2 = \frac{p_s^2}{1 + k_{eq} \left(\frac{T}{C} \right)}$$

Static sag $T = F_o / K_{rot}$



Rotor flexibility decreases system natural frequency, thus lowering threshold speed of instability. **WFR still = 0.50**

Figure 21



PHYSICS of WHIRL MOTION

Forces in rotating coordinate system

$$\begin{pmatrix} F_r \\ F_t \end{pmatrix}_d = - \begin{bmatrix} K_{rr} & K_{rt} \\ K_{tr} & K_{tt} \end{bmatrix} \begin{pmatrix} \Delta e \\ e_0 \Delta \phi \end{pmatrix} - \begin{bmatrix} C_{rr} & C_{tr} \\ C_{tr} & C_{tt} \end{bmatrix} \begin{pmatrix} \Delta \dot{e} \\ e_0 \Delta \dot{\phi} \end{pmatrix}$$

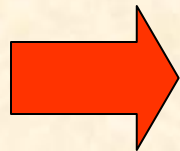
Bearing force coefficients at (e/c)=0

$$K_{rr} = K_{tt} = C_{rt} = C_{tr} = 0$$

$$\bar{K} = K_{rt} = -K_{tr} = \frac{\Omega}{2} \bar{C}; \quad \bar{C} = C_{tt} = C_{rr} = \frac{\mu R L^3}{C^3} \frac{\pi}{2}$$

Resultant forces

$$F_{r_d} = 0; \quad F_{t_d} = -(C_{tt} \omega - K_{rt}) \Delta e$$



At centered condition: No radial support, tangential force must be < 0 to oppose whirl motion

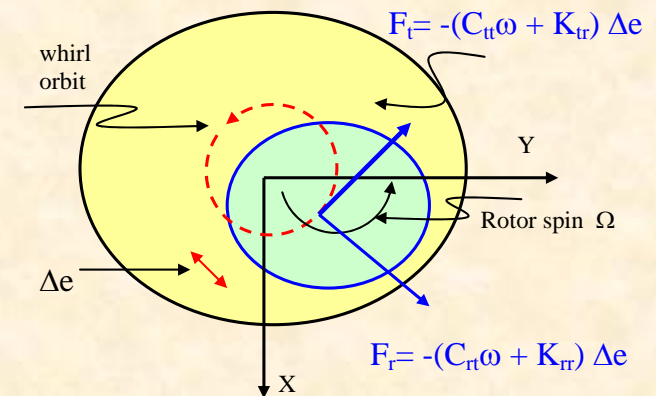
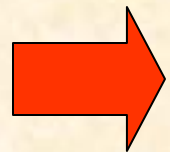
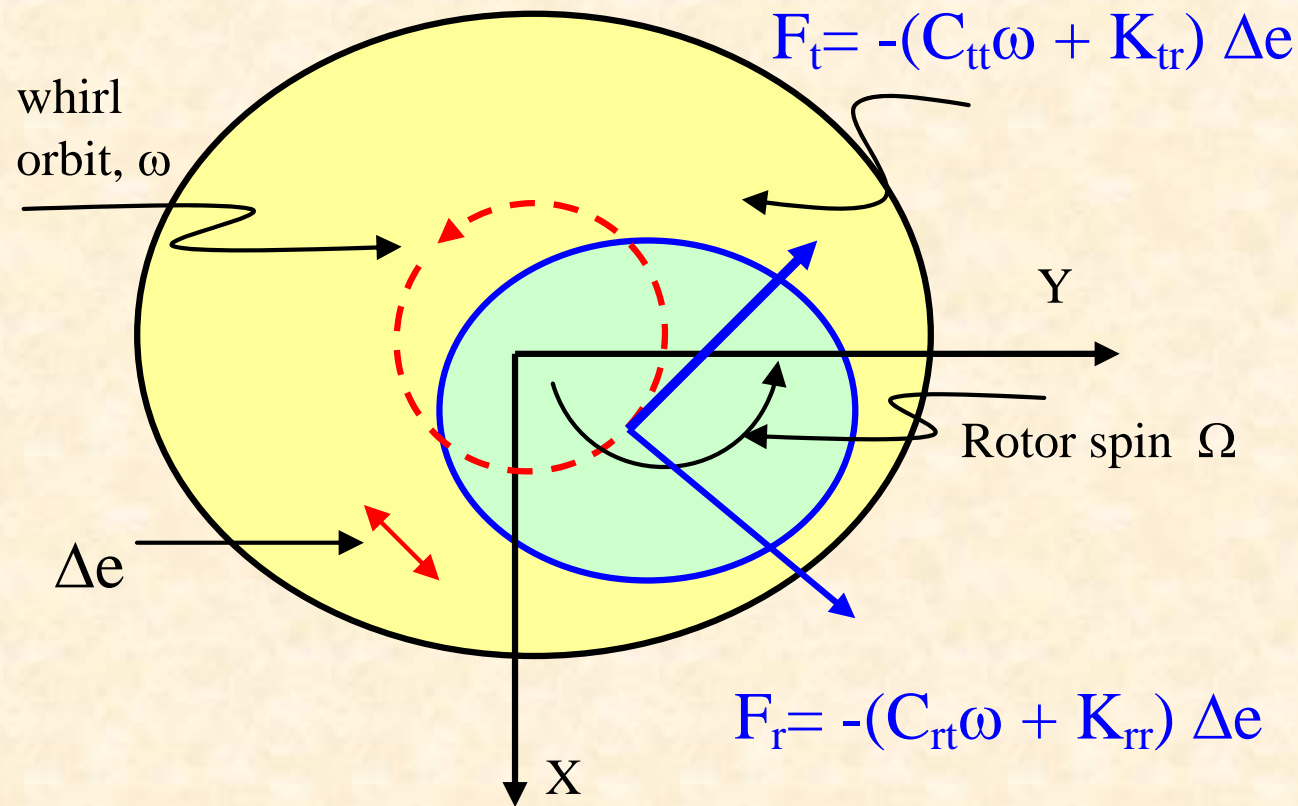


Figure 22



PHYSICS of WHIRL MOTION



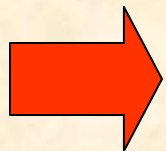
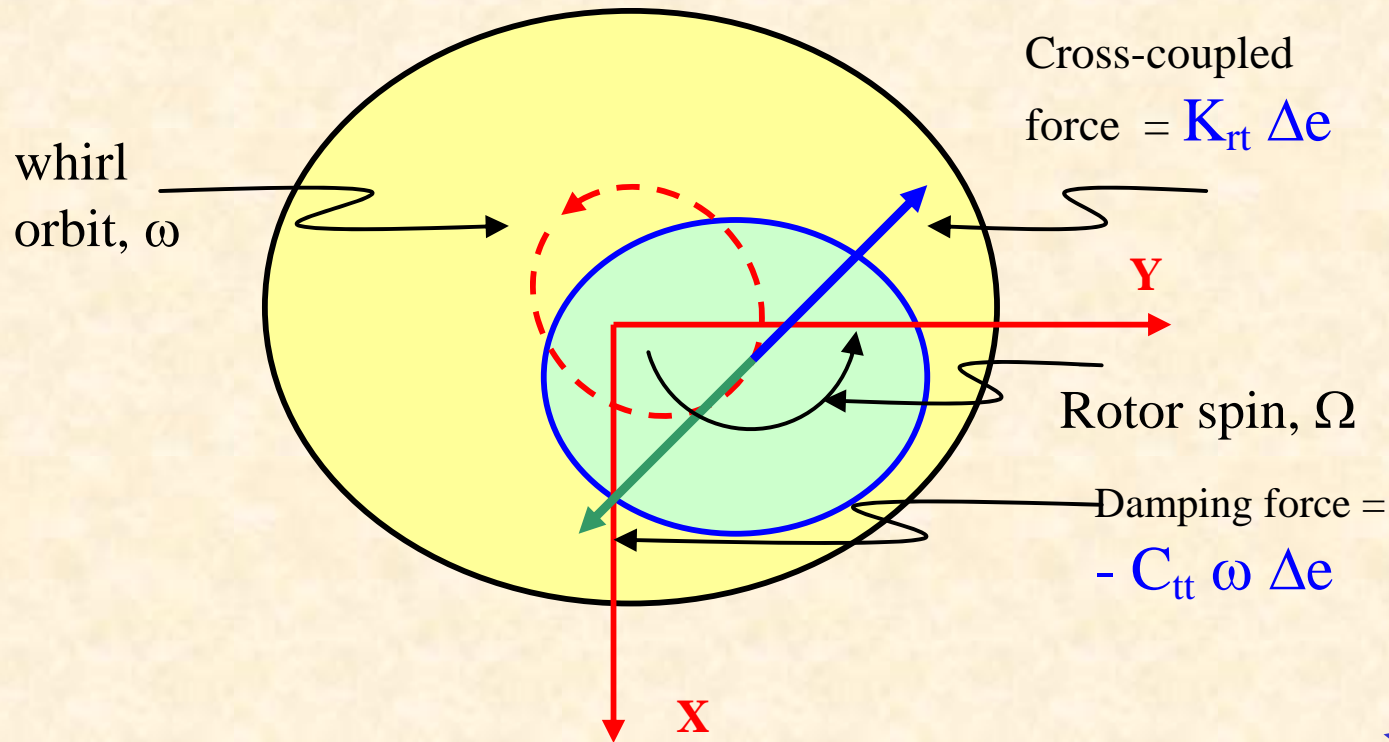
$$(C_{tt} - \frac{1}{\omega} K_{rt}) = C_{eq} < 0$$

Loss of damping for
speeds above ω_s

Figure 22 Force diagram for circular centered whirl motions



PHYSICS of WHIRL MOTION



$$(C_{tt} - \frac{1}{\omega} K_{rt}) = C_{eq} < 0$$

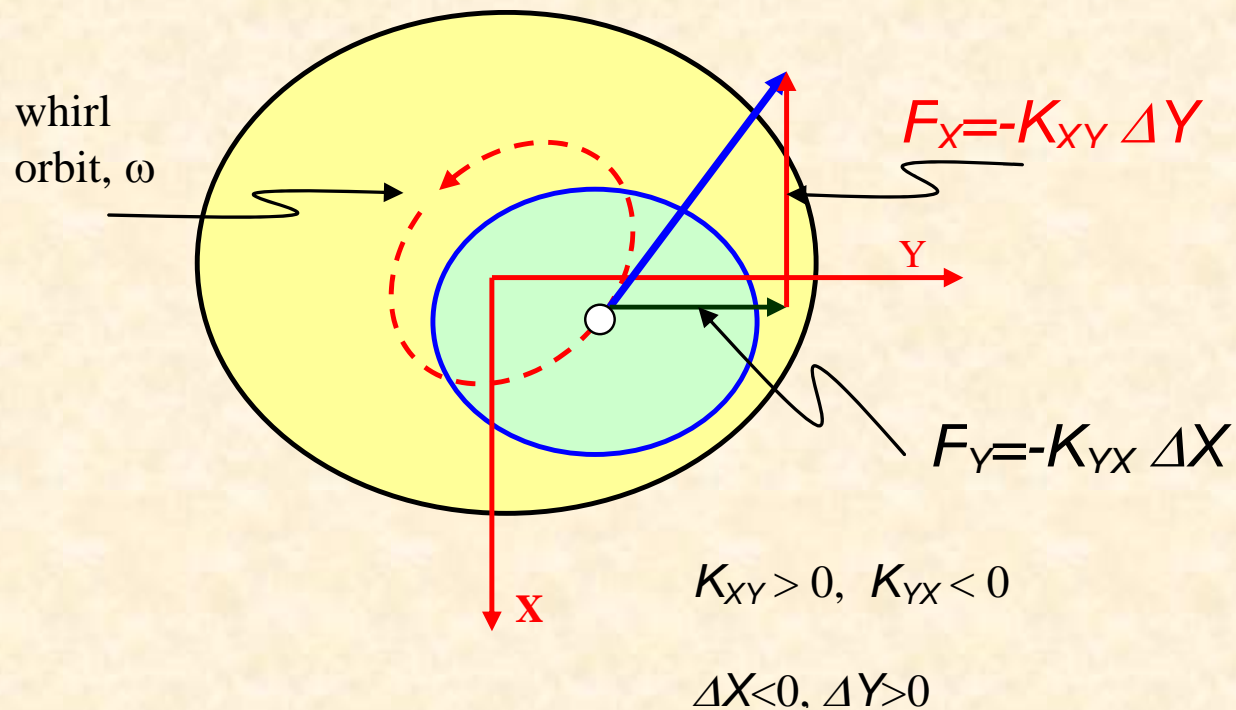
Cross-coupled force is a FOLLOWER force



Figure 23 Forces driving and retarding rotor whirl motion



PHYSICS of WHIRL MOTION

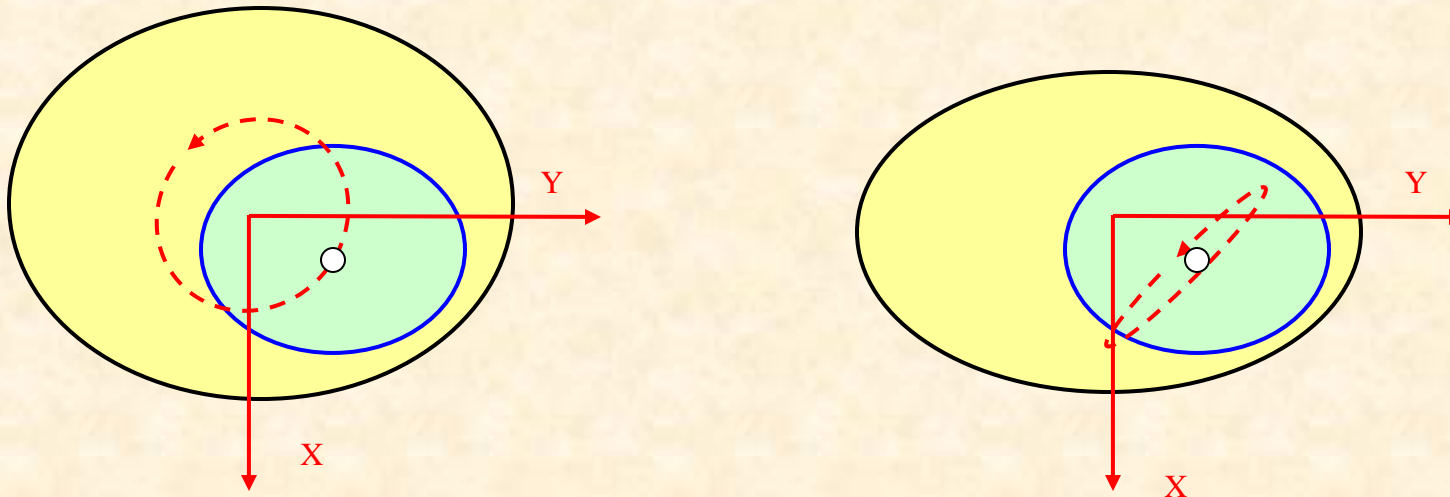


➔
$$E = -\left(2\pi \Delta e^2\right)(C_{tt} \omega - K_{rt}) = -2Area_{orbit} C_{eq} \omega$$

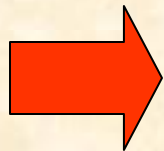
Work from bearing forces. $E < 0$ is dissipative; $E > 0$ adds energy to whirl motion



PHYSICS of WHIRL MOTION



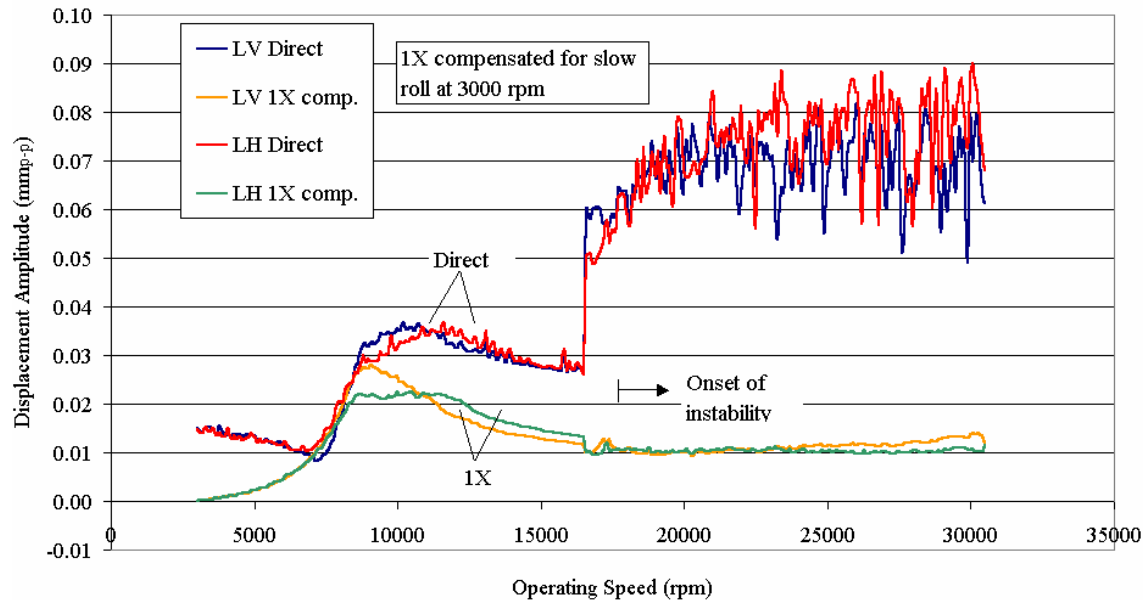
Energy from cross-coupled forces = **Area** ($K_{xy} - K_{yx}$)



Bearing asymmetry creates strong stiffness asymmetry – a remedy to reduce potential for hydrodynamic instability

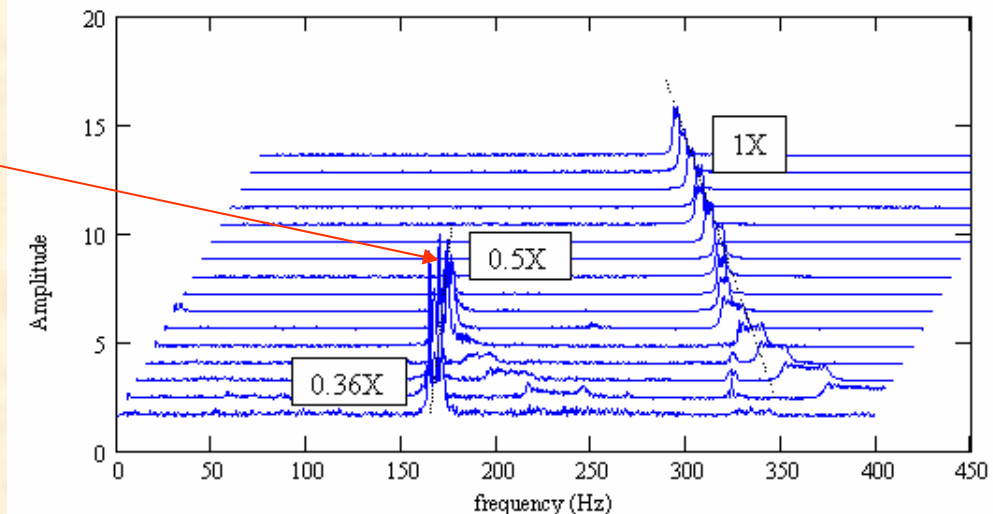


EXPERIMENTAL EVIDENCE of INSTABILITY



Amplitudes of rotor motion versus shaft speed. Experimental evidence of rotordynamic instability

Waterfall of recorded rotor motion demonstrating subsynchronous whirl

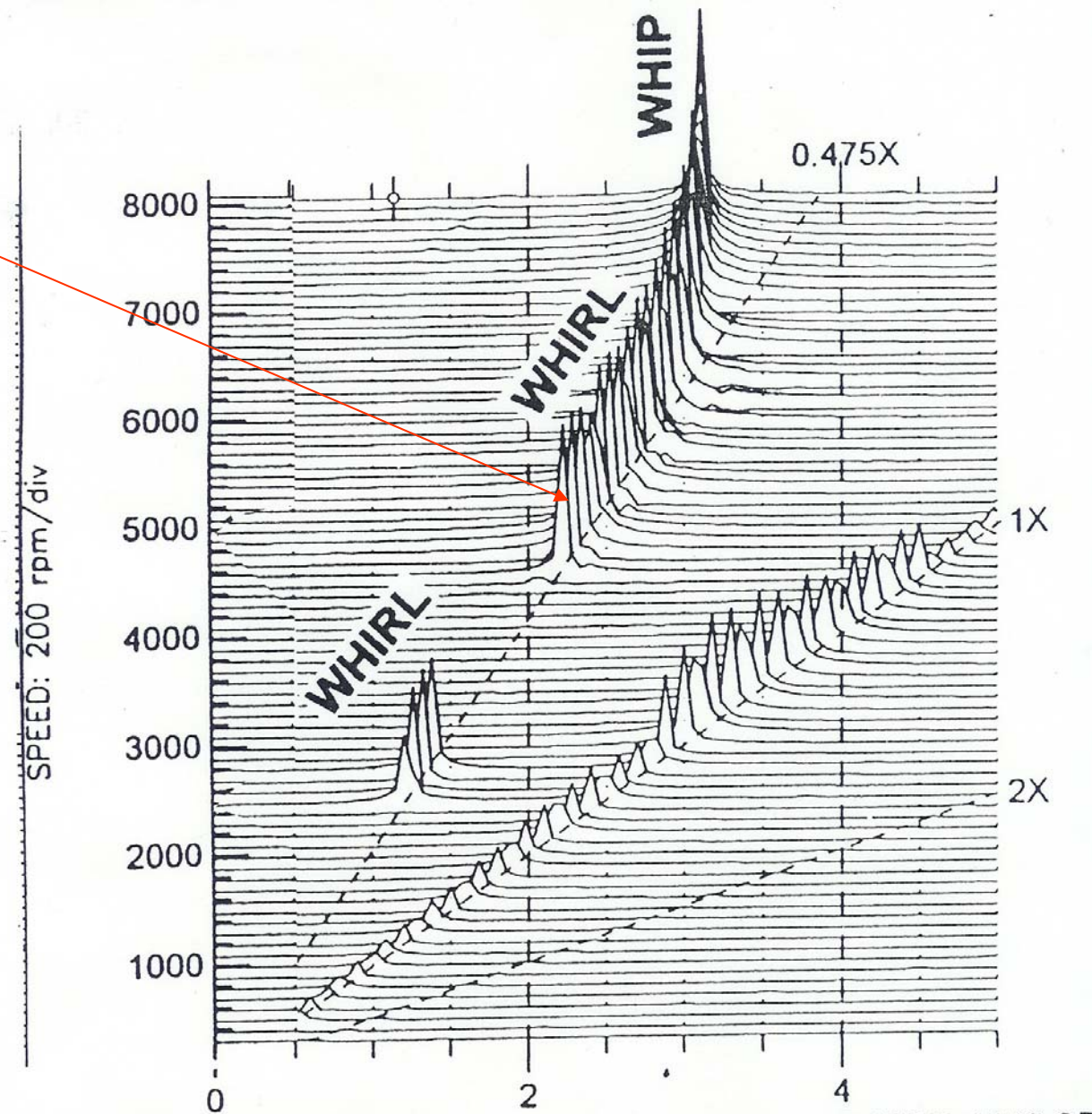




EXPERIMENTAL EVIDENCE of INSTABILITY

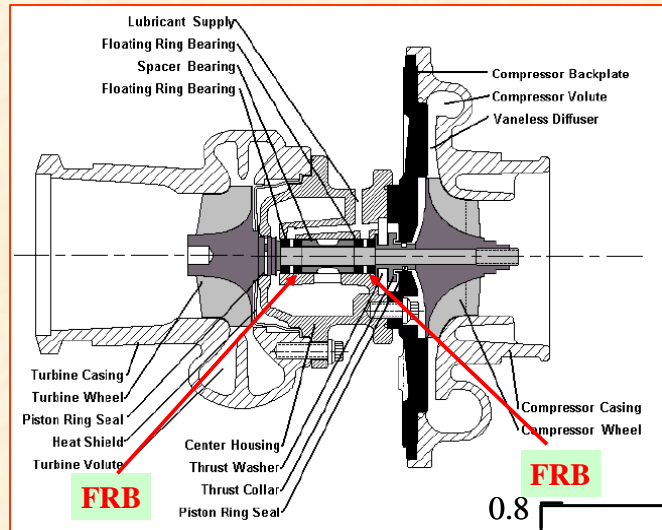
WFR $\sim 0.47 X$

Transition from
oil whirl to **oil
whip** (sub sync
freq. locks at
system natural
frequency)



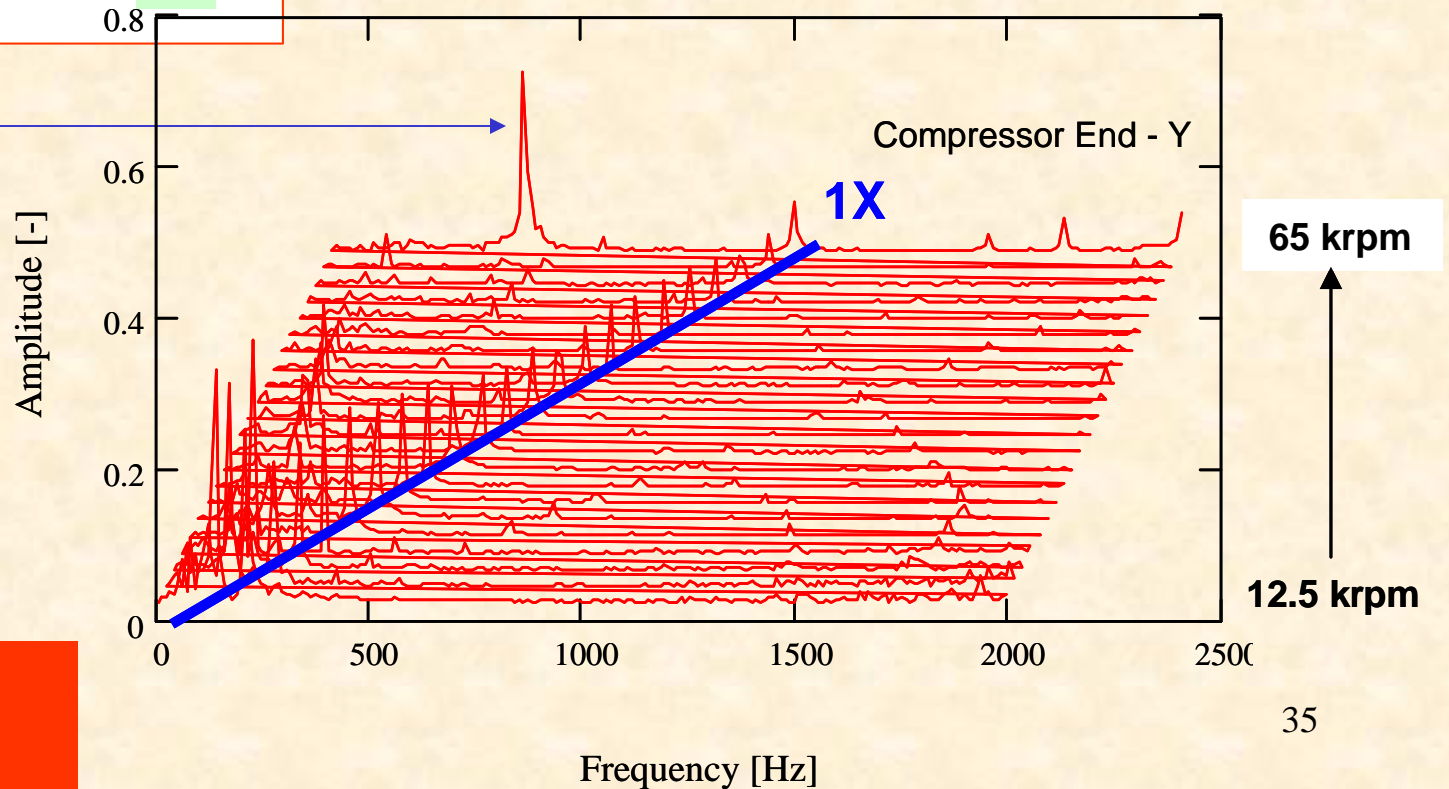


EXPERIMENTAL EVIDENCE of INSTABILITY



TC supported on floating ring bearings

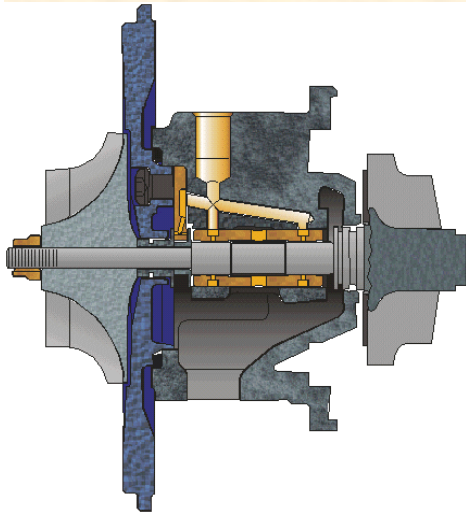
WFR ~ 0.50 X



**Automotive
Turbocharger**

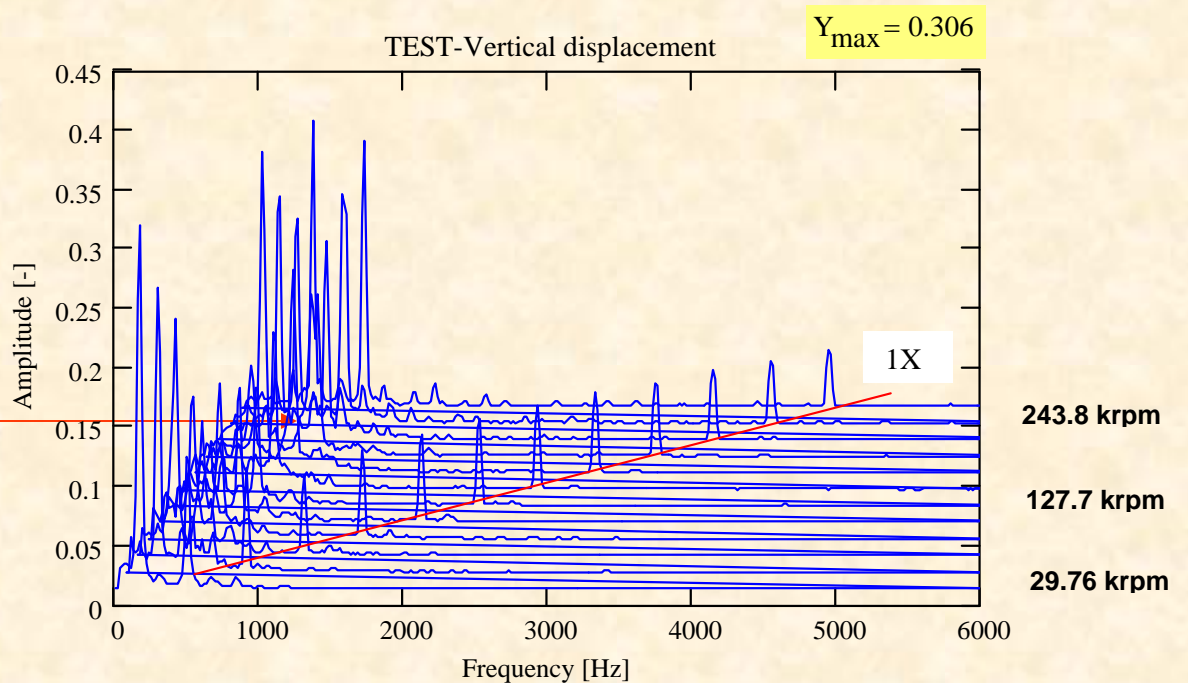


EXPERIMENTAL EVIDENCE of INSTABILITY



TC supported on semi-floating ring bearings

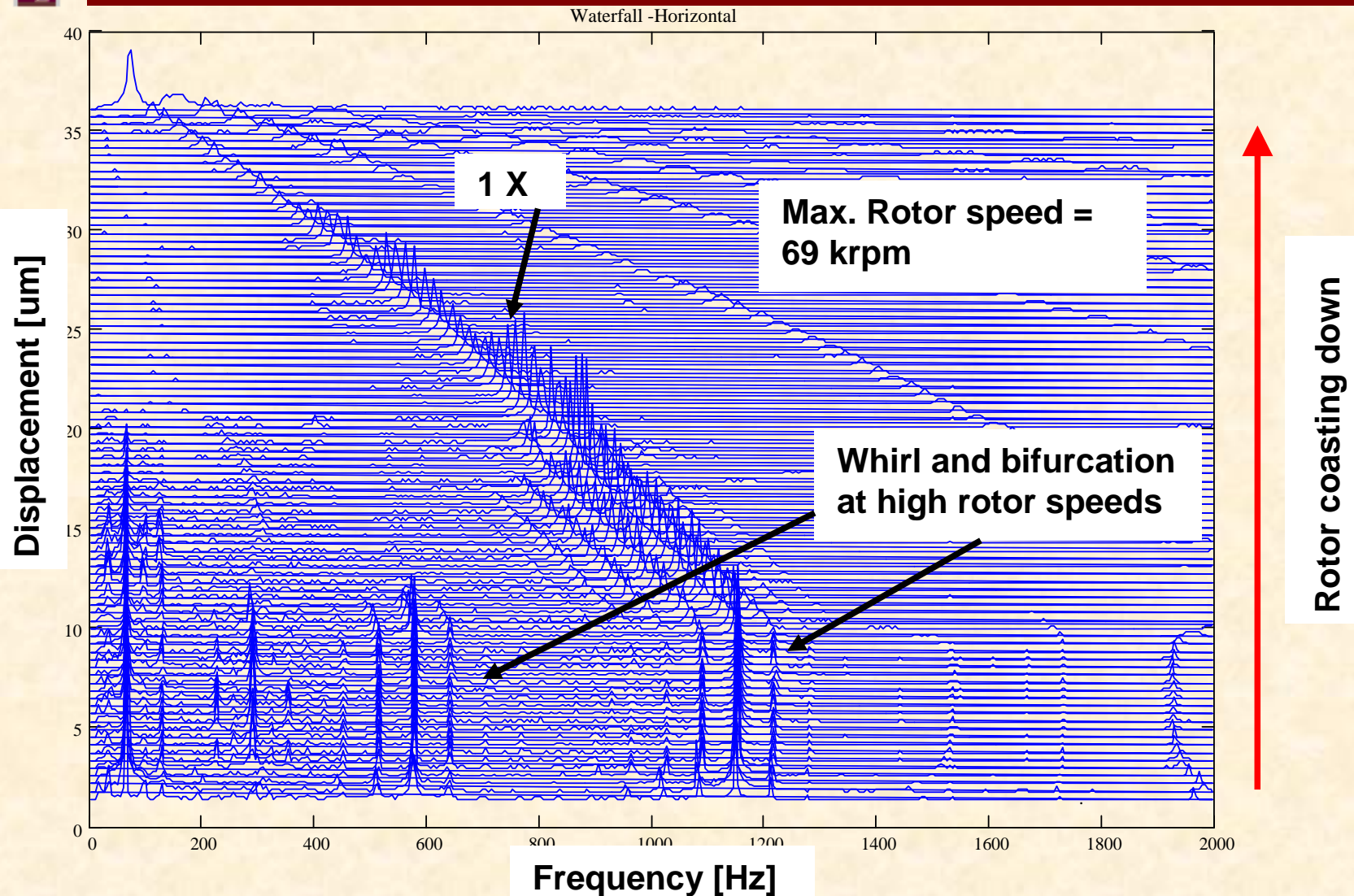
Multiple sub-synchronous motions



**Automotive
Turbocharger**



EXPERIMENTAL EVIDENCE of INSTABILITY



Metal Mesh Gas Foil Bearing



CLOSURE

Commercial rotating machinery implements bearing configurations aiming to reduce and even eliminate the potential of hydrodynamic instability (sub synchronous whirl)

Cutting axial grooves in the bearing to supply oil flow into the lubricated surfaces generates some of these geometries.

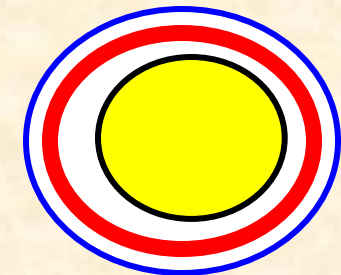
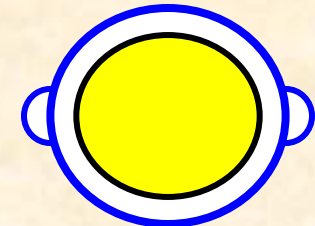
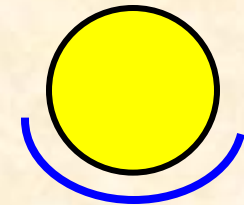
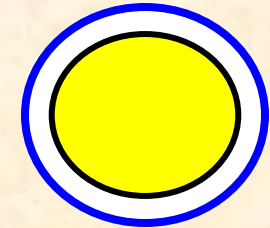
Other bearing types have various patterns of variable clearance (preload and offset) to create a **pad film thickness that has strongly converging wedge, thus generating a direct stiffness for operation even at the journal centered position.**

In tilting pad bearings, each pad is able to pivot, enabling its own equilibrium position. This feature results in a strongly converging film region for each loaded pad and the **near absence of cross-coupled stiffness coefficients.**



OTHER BEARING GEOMETRIES

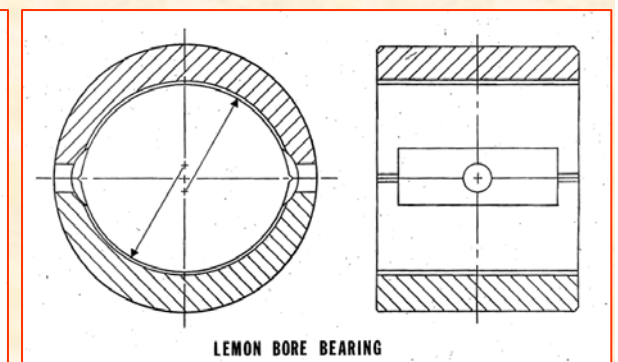
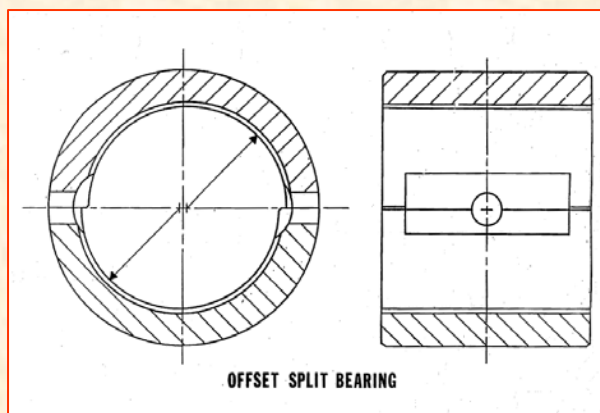
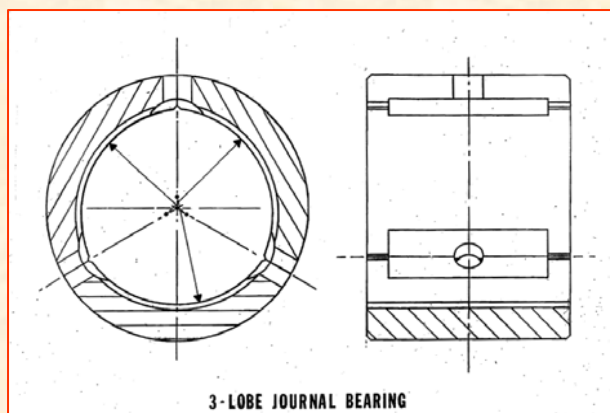
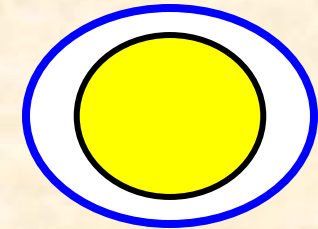
Bearing Type	Advantages	Disadvantages	Comments
Plain Journal	1. Easy to make 2. Low Cost	1. Most prone to oil whirl	Round bearings are nearly always "crushed" to make elliptical bearings
Partial Arc	1. Easy to make 2. Low Cost 3. Low horsepower loss	1. Poor vibration resistance 2. Oil supply not easily contained	Bearing used only on rather old machines
Axial Groove	1. Easy to make 2. Low Cost	1. Subject to oil whirl	Round bearings are nearly always "crushed" to make elliptical or multi-lobe
Floating Ring	1. Relatively easy to make 2. Low Cost	1. Subject to oil whirl (two whirl frequencies from inner and outer films (50% shaft speed, 50% [shaft + ring] speeds))	Used primarily on high speed turbochargers for PV and CV engines





OTHER BEARING GEOMETRIES

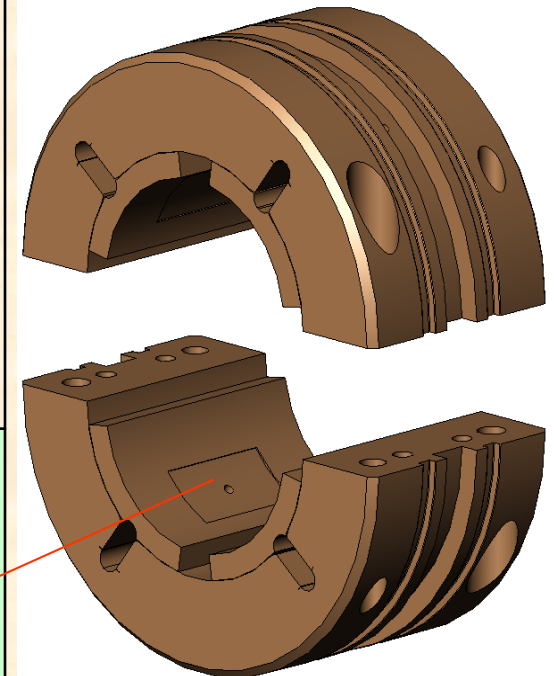
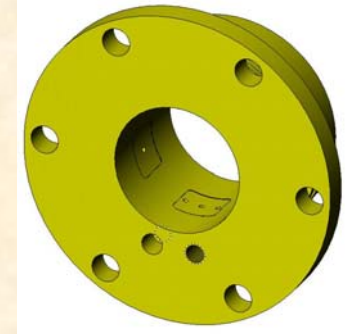
Bearing Type	Advantages	Disadvantages	Comments
Elliptical	1. Easy to make 2. Low Cost 3. Good damping at critical speeds	1. Subject to oil whirl at high speeds 2. Load direction must be known	Probably most widely used bearing at low or moderate rotor speeds
Offset Half (With Horizontal Split)	1. Excellent suppression of whirl at high speeds 2. Low Cost 3. Easy to make	1. Fair suppression of whirl at moderate speeds 2. Load direction must be known	High horizontal stiffness and low vertical stiffness - may become popular - used outside U.S.
Three and Four Lobe	1. Good suppression of whirl 2. Overall good performance 3. Moderate cost	1. Expensive to make properly 2. Subject to whirl at high speeds	Currently used by some manufacturers as a standard bearing design





OTHER BEARING GEOMETRIES

Bearing Type	Advantages	Disadvantages	Comments
Pressure Dam (Single Dam)	<ol style="list-style-type: none"> 1. Good suppression of whirl 2. Low cost 3. Good damping at critical speeds 4. Easy to make 	<ol style="list-style-type: none"> 1. Goes unstable with little warning 2. Dam may be subject to wear or build up over time 3. Load direction must be known 	Very popular in the petrochemical industry. Easy to convert elliptical over to pressure dam
Multi-Dam Axial Groove or Multiple-Lobe	<ol style="list-style-type: none"> 1. Dams are relatively easy to place in existing bearings 2. Good suppression of whirl 3. Relatively low cost 4. Good overall performance 	<ol style="list-style-type: none"> 1. Complex bearing requiring detailed analysis 2. May not suppress whirl due to non bearing causes 	Used as standard design by some manufacturers
Hydrostatic	<ol style="list-style-type: none"> 1. Good suppression of oil whirl 2. Wide range of design parameters 3. Moderate cost 	<ol style="list-style-type: none"> 1. Poor damping at critical speeds 2. Requires careful design 3. Requires high pressure lubricant supply 	Generally high stiffness properties used for high precision rotors





OTHER BEARING GEOMETRIES

Bearing Type	Advantages	Disadvantages	Comments
Tilting Pad journal bearing Flexure pivot, tilting pad bearing	1. Will not cause whirl (no cross coupling)	1. High Cost 2. Requires careful design 3. Poor damping at critical speeds 4. Hard to determine actual clearances 5. Load direction must be known	Widely used bearing to stabilize machines with subsynchronous non-bearing related excitations
Foil bearing	1. Tolerance to misalignment. 2. Oil-free	1. High cost. 2. Dynamic performance not well known for heavily loaded machinery. 3. Prone to subsynchronous whirl	Used mainly for low load support on high speed machinery (APU units).

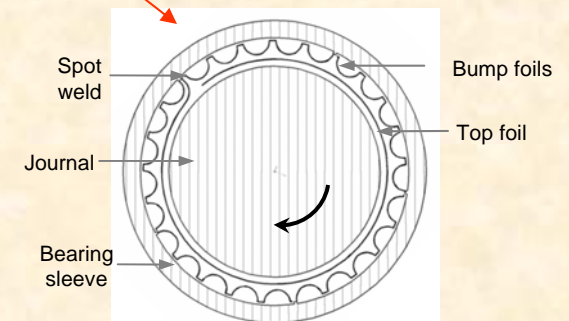
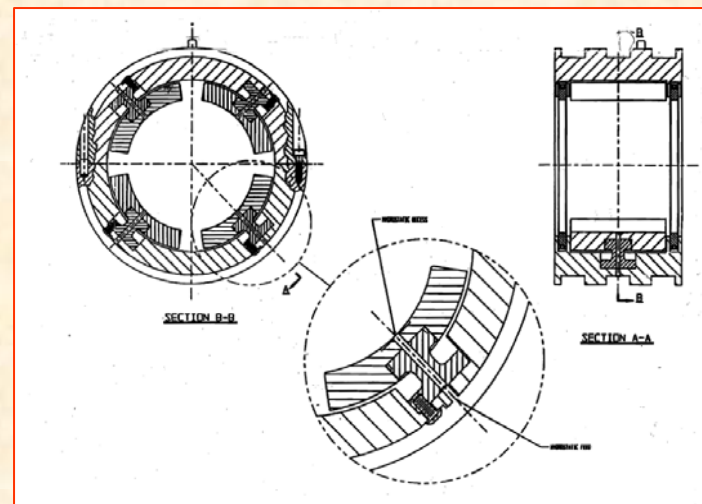
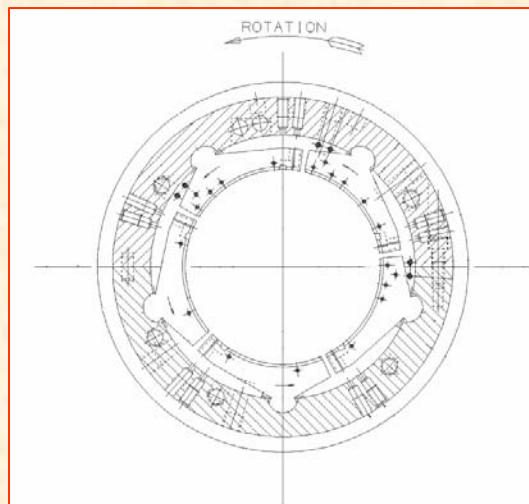


Table 3 Tilting Pad Bearings & Foil Bearings